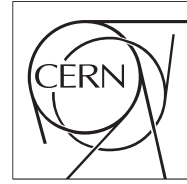




The Compact Muon Solenoid Experiment

Detector Note

The content of this note is intended for CMS internal use and distribution only



2023/06/08

Archive Hash: caa5f0f-D

Archive Date: 2023/06/05

The L1 Track Trigger Upgrade: Properties, Efficiencies, and Rates for Track Stubs

Reza Goldouzian¹, Mike Hildreth¹, Alexander Morton², and Austin Townsend¹

¹ University of Notre Dame (US)

² Vrije Universiteit Brussel (US)

Abstract

A new CMS tracker detector will be installed for the High Luminosity LHC. The new tracker will read out hits at a sufficiently high rate to allow track reconstruction in real time. This will allow the inclusion of tracking information in the Level 1 (L1) trigger system for the first time, dramatically lowering the CMS L1 trigger rate. Stubs are building blocks of the L1 trigger system. Therefore, determination and measurement of the stub properties are crucial tasks. In this note, we study various features of stubs for the CMS experiment phase II track trigger upgrade including stub rates, stub construction efficiency, stub transmission efficiency, stub bend decoding, etc. Consequently, new stub window tunes are proposed which have high stub construction efficiencies with the lowest possible rates. Additionally we present a new method of stub bend decoding which can cope with changing stub window sizes. This work is based on a full simulation of LHC events with high pileup.

This box is only visible in draft mode. Please make sure the values below make sense.

PDFAuthor: Reza Goldouzian, Mike Hildreth and Austin Townsend
PDFTitle: The L1 Track Trigger Upgrade: Properties, Efficiencies, and Rates for Track Stubs
PDFSubject: CMS
PDFKeywords: CMS, track trigger

Please also verify that the abstract does not use any user defined symbols

1 Introduction

The goal of the High-Luminosity LHC program is to collect an integrated luminosity of 3000 fb^{-1} in about ten years of operations starting in 2028 and with a peak luminosity of $7.5 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$. As the bunch crossing separation will stay the same as today (25 ns), the increase of instantaneous luminosity will result in up to 200 inelastic proton-proton collisions per bunch crossing (pileup). The CMS detector needs to be substantially upgraded in order to exploit the increase in luminosity provided by the HL-LHC [1].

A major new functionality of the CMS detector for the HL-LHC is the inclusion of data from the Outer Tracker (OT) in the L1 trigger, facilitated by the readout of silicon tracking information at an unprecedented 40 MHz data rate [2]. The primary function that enables this improvement is the ability to perform local transverse momentum (p_T) measurements with the detector front-end electronics. Studies have shown that 97% (99%) of the particles created in pp interactions at 14 TeV have $p_T < 2 \text{ GeV}$ ($p_T < 3 \text{ GeV}$). The readout rate of soft interactions can be reduced by a factor of 10 via selections on the local p_T measurements [2].

New tracking modules utilize a pair of closely spaced silicon sensors (1.6 – 4.0 mm) and on-detector correlation logic in order to discriminate charged particle tracks with a p_T exceeding a threshold of 2-3 GeV. Two module types are foreseen for the OT:

- PS modules: A PS module is composed of one strip sensor (two rows of 960 AC-coupled strips with dimensions $2.35 \text{ cm} \times 100 \mu\text{m}$) and a one macro-pixel sensor (30 720 DC-coupled pixels with dimensions $1.5 \text{ mm} \times 100 \mu\text{m}$).
- 2S modules: A 2S module is composed of two strip sensors (two rows of 1016 AC-coupled strips with dimensions $5 \text{ cm} \times 90 \mu\text{m}$ per sensor).

The OT is arranged in a barrel made of two subsystems, TBPS for the innermost 3 layers and TB2S for the outermost 3 layers, and 5(x2) endcap discs (TEDD). The OT will cover a surface of about 192 m^2 for a total of 42M strip and 170M macro pixel channels. The PS modules are deployed in the first three layers of the Outer Tracker, in the radial region of 200 – 600 mm and in rings on disc-like structure in the endcaps up to radii 700 mm [3]. The 2S modules are deployed in the outermost three layers in Barrel (in the radial region above 600 mm) and in the large radii rings in the endcaps. The proposed layout of the Tracker is shown in Fig.1.

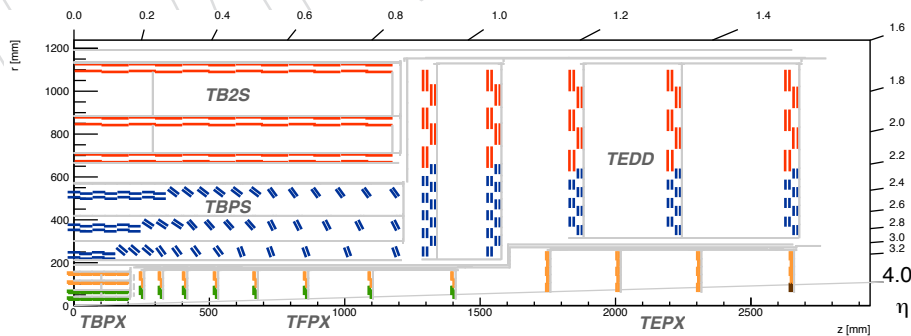


Figure 1: Sketch of one quarter of the layout of the CMS Tracker for HL-LHC in the $r - z$ view. Inner Tracker 1x2 and 2x2 readout chips modules are shown in green and yellow respectively, Outer Tracker PS and 2S modules in blue and red.

Pairs of closely spaced detector layers are inspected to see if they have pairs of clusters consistent with the passage of a high momentum particle. For each hit in the inner layer (closer to the interaction point), a window is opened on the outer layer. If a hit is found within the window, a stub is generated. Each stub consists of a position and a rough p_T measurement. Sketch of a

34 p_T -module showing the concept of stub is shown in Fig. 2.

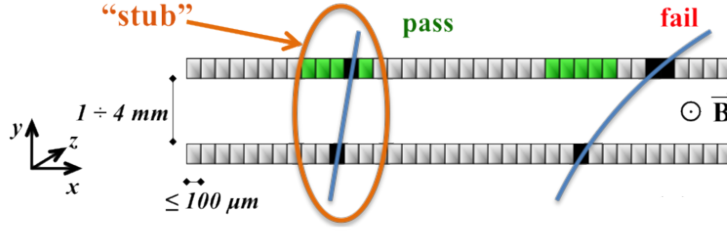


Figure 2: Sketch of a p_T -module showing the concept of stub selection.

35 To perform stub correlation in the 2S modules, the signals of the top and bottom sensor are
 36 routed to the same CMS binary chip (CBC), which performs the correlation logic. This is possi-
 37 ble by folding the readout hybrids around a stiffener. In the PS modules, strip signals are
 38 processed by the strip-sensor ASIC (SSA), and macro-pixel signals by the macro-pixel ASIC
 39 (MPA). The strip data is routed from the SSA to the MPA via a folded hybrid, which then per-
 40 forms the cluster correlation. A detailed description of the front-end electronics can be found
 41 in [3]. One 2S front-end hybrid carries eight CBCs reading out the strips of the top and bot-
 42 tom sensors at one sensor end, plus the Concentrator Integrated Circuit (CIC), which serves
 43 as interface between all the CBCs of the hybrid and the readout link. The role of the CIC is
 44 mainly to aggregate and serialize the data of the readout chips and to distribute clock, trigger,
 45 and control signals to them. One PS front-end hybrid houses eight SSAs reading out the strip
 46 sensor, and the same CIC as used for 2S hybrids. All the front-end chips implement binary
 47 readout. Images of the 2S and PS modules are shown in Figure 3.

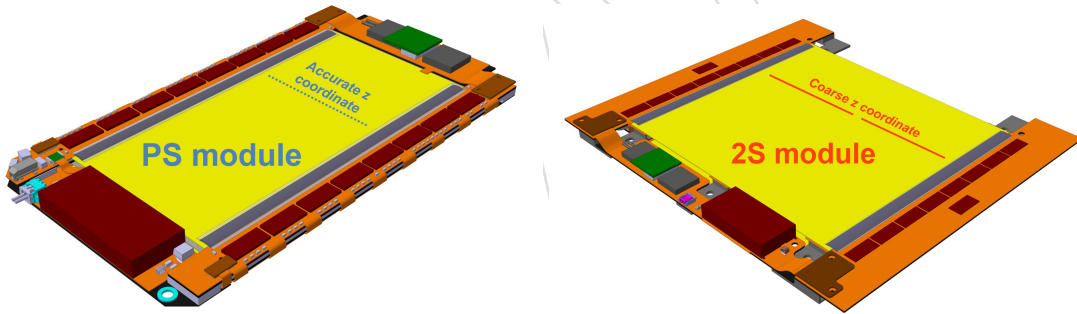


Figure 3: The 2S module (left) and PS module (right) of the Outer Tracker.

48 The data flow is organized in two separate paths: L1 readout (DAQ) and Trigger (TRIG). Each
 49 CBC generates high p_T stub data at bunch crossing (BX) rate. The CBCs exchange data with
 50 their neighbors to identify clusters spanning across chip boundaries. At a data transfer rate of
 51 320 Mb/s, each CBC chip sends 1 bit of DAQ and 5 bit of TRIG data to the concentrator every
 52 3.125 ns. This bandwidth is compatible with transferring up to three trigger stubs from each
 53 CBC every BX, and sending unsparsified readout data from each CBC pipeline up to an aver-
 54 age L1-accept rate of 750 kHz. The transfer scheme and data formats in PS module are very
 55 similar to those used in the 2S module. The data transfer bandwidth is compatible with trans-
 56 ferring up to five trigger stubs from each MPA every 2 BX, and sending all sparsified readout
 57 data from each MPA pipeline up to a 750 kHz L1-accept rate with negligible loss. CBCs/MPAs
 58 send out stubs to the CIC. The CIC format them into data packets containing the trigger in-
 59 formation from eight BX and the raw data from events passing the Level 1 (L1) trigger, before
 60 transmission to the Low-power Gigabit Transceiver (lpGBT). Due to the available CIC band-
 61 width, additional stubs are discarded, but stubs are sorted such as to keep those with lower

bending, presumably corresponding to tracks with higher p_T . The format of the CIC trigger block has been described in details in [4]. The CIC bandwidth can be adjusted to the module local occupancy by configuring the data rate (5.12 Gb/s or 10.24 Gb/s raw data rate, also referred to as 5G and 10G) and/or the forward error correction (FEC) level (FEC5 or FEC12, up to five or twelve consecutive bits in error can be corrected). This tuneability is used to increase bandwidth where expected data rates are very high, at the expense of increased power dissipation and decreased error correction level. In Figure 4, layers and rings with 5G or 10G are shown. In the current simulation code (see L1Trigger/TrackTrigger/python/TTStub_cfi.py), the following limits on number of transferred stubs are considered based on the mentioned bandwidths.

- CBCLimit = cms.uint32(3), CBC chip limit (in stubs/chip/BX)
- MPALimit = cms.uint32(5), MPA chip limit (in stubs/chip/2BX)
- SS5GCICLimit = cms.uint32(16), 2S 5G chip limit (in stubs/CIC/8BX)
- PS5GCICLimit = cms.uint32(16), PS 5G chip limit (in stubs/CIC/8BX)
- PS10GCICLimit = cms.uint32(35), PS 10G chip limit (in stubs/CIC/8BX)

If number of stubs are more than CBC/MPA/CIC transfer threshold in 1/2/8 BX, they will not transfer to the next step. The rate of stubs that are lost because of the bandwidth of CBC/MPA/CIC are called "CBC/MPA/CIC fail" in this note.

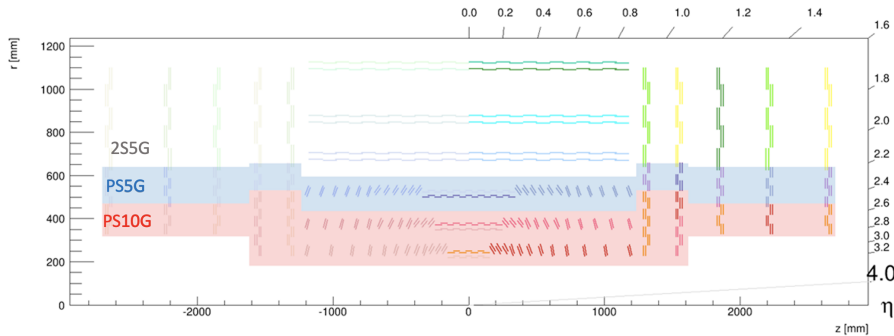


Figure 4: Modules with 5G and 10G data rate.

2 Samples

The samples used here have been produced by CMSSW 11.3.0 and are listed in table 1. The detector geometry considered is the D76 (=T21 tracker).

Table 1: List of simulated samples (see https://twiki.cern.ch/twiki/bin/view/CMS/L1TrackMC#RelVal_MC_samples).

sample	PU	p_T	N	DAS name
t \bar{t}	0	-	10k	/RelValTTbar_14TeV/CMSSW_11.3.0-113X_mcRun4_realistic_v7_2026D76noPU-v1
t \bar{t}	200	-	9k	/RelValTTbar_14TeV/CMSSW_11.3.0.pre6-PU_113X_mcRun4_realistic_v6_2026D76PU200-v1
Single electron	0	2-100	100k	/RelValSingleEFlatPt2To100/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v2
Single electron	0	1.5-8	100k	/RelValSingleElectronFlatPt1p5To8/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v1
Single muon	0	2-100	100k	/RelValSingleMuFlatPt2To100/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v1
Single muon	0	1.5-8	100k	/RelValSingleMuFlatPt1p5To8/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v1
Displaced muon	0	2-100	100k	/RelValDisplacedMuPt2To100Dxy100/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v1
Displaced muon	0	1.5-8	100k	/RelValDisplacedMuPt1p5To8Dxy100/CMSSW_11.3.0.pre6-113X_mcRun4_realistic_v6_2026D76noPU-v1

3 Stub rates

The stub rate is an important parameter for both the front-end and back-end electronics. At the front-end it is important to check that the average stub rate per module is well within the readout capacity of the detector. At the back-end, the stub multiplicity per trigger tower will impact directly the performance of the L1 tracking system, and must therefore stay under control.

Each stub is built from two clusters. Clusters are categorized into “genuine”, “combinatoric” and “unknown” based on their matching condition to the tracking particles (TP). If cluster is matched to only one tracking particle or a single TP has more than 99% of the total p_T of all TP associated to the cluster, cluster is called genuine. If more than one TP are matched to the cluster and non of them has more than 99% of the total p_T of all TP, cluster is called combinatoric. If no TP is matched, cluster is called unknown. See <https://twiki.cern.ch/twiki/bin/viewauth/CMS/SLHCTrackerTriggerSWTools> for more details. Stubs that are made from these three cluster types are called “genuine”, “combinatoric” and “unknown” according to the following criteria;

- If both clusters are unknown, the stub is unknown.
- If only one cluster is unknown, the stub is combinatoric.
- If both clusters are genuine, and are associated to the same (main) TP, the stub is genuine.
- If both clusters are genuine, but are associated to different (main) TP, the stub is combinatoric.
- If one cluster is combinatoric and the other is genuine/combinatoric, and they both share exactly one TP in common, then the stub is genuine. (The clusters can have other TP besides the shared one, as long as these are not shared). If instead the clusters share 0 or 2 TP in common, then the stub is combinatoric.

In Figure 5, stub rates per BX (PBX) and stub rate per BX per module (PBXPmodule) are shown for all, genuine, combinatoric, and unknown stubs for $t\bar{t}$ events with 200 PU. In Figure 6, stub rate per BX per module is shown as a function of module η , ρ and z . Two dimensional plots where each bin corresponds to a module is shown in Figures 7 and 8 for barrel layers and endcap disks respectively.

As was discussed in the previous section, stubs can be lost because of the limited bandwidth of the CBC/MPA/CIC data transfer. In Figure 9-10, fractions of all stubs that are failed by the CBC/MPA/CIC are shown. Less than 2×10^{-3} of stubs are failed by the MPAs/CBCs in the first three layers of the TB and in all TE disks. In TB2S, up to 5% of stubs are failed by the CBC which is too much. We have compared the fraction of failed stubs that are genuine to the combinatoric and unknown stubs in Figure 11. Genuine stubs that are lost in the last three layers are 1-1.5 % of total genuine stubs. In addition, most of these stubs are from low p_T TPs. In figure 12, fractions of genuine stubs with $p_T > 2$ GeV (p_T of the matched TP) that are failed by the CBC/MPA are compared to those for all and genuine stubs. It can be seen that for genuine stubs with $p_T > 2$ GeV, the fraction rates are around 0.2%. In addition, CIC fail rates are well below 0.1% in all detector regions. Therefore, the designed CBC/MPA (CIC) bandwidth lead up to 0.2% (0.1%) inefficiencies for high p_T genuine stubs.

It is worth mentioning that our simulation of the FE inefficiencies is not really accurate. We are summing hits from $t\bar{t}$ + 200PU over the bunch crossings, whereas we should have just pileup in the bunches previous to the $t\bar{t}$ event. For this high an occupancy, its probably not a big

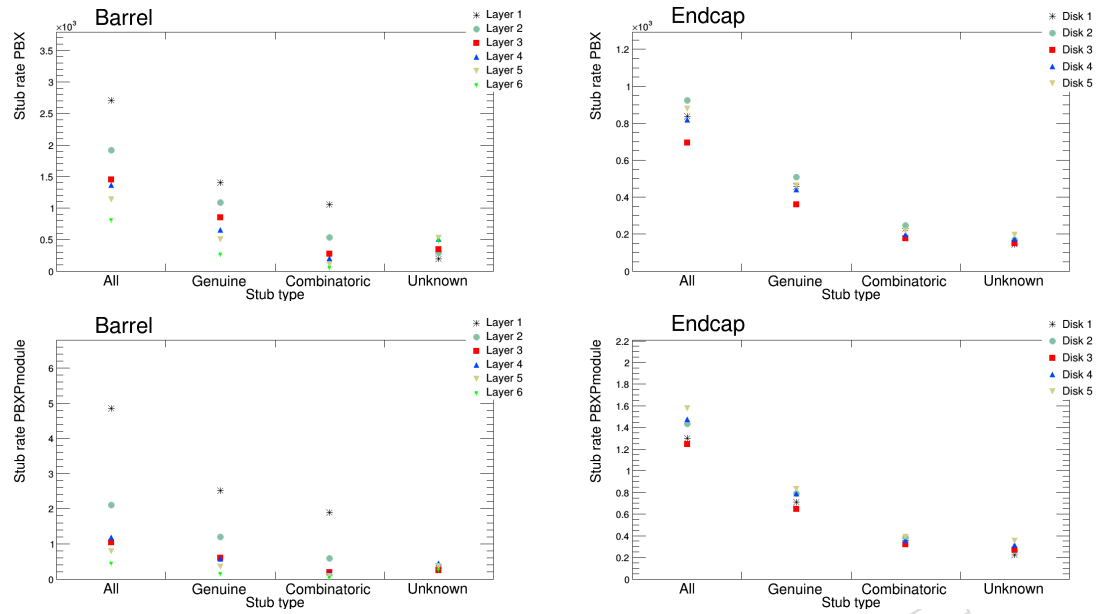


Figure 5: Stub rates per BX and stub rates per BX per module in barrel (left) and endcap (right) are shown for all, genuine, combinatoric and unknown stubs for $t\bar{t}$ events with 200 PU.

128 effect. But, it means these numbers are pessimistic.

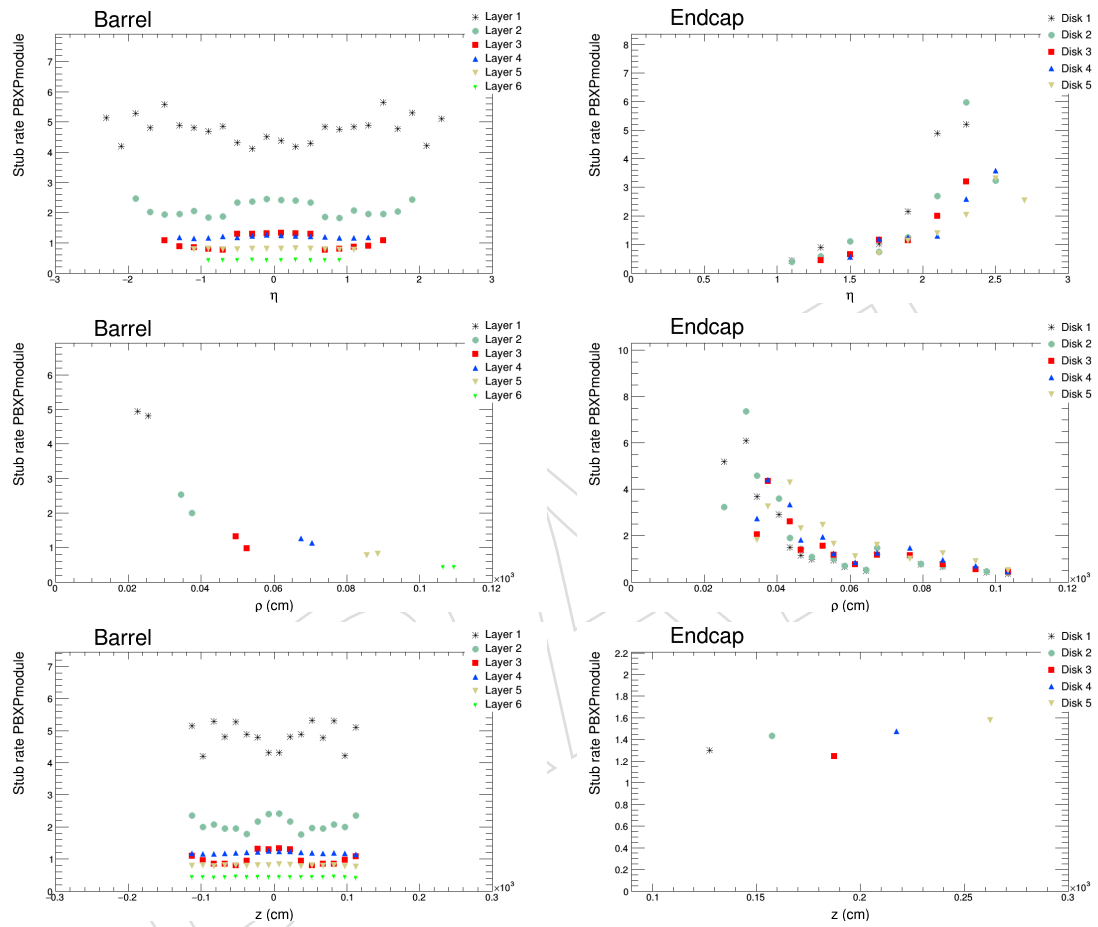


Figure 6: Stub rates per BX per module in barrel (left) and endcap (right) are shown for all stubs as a function of module η , ρ and z using $t\bar{t}$ events with 200 PU.

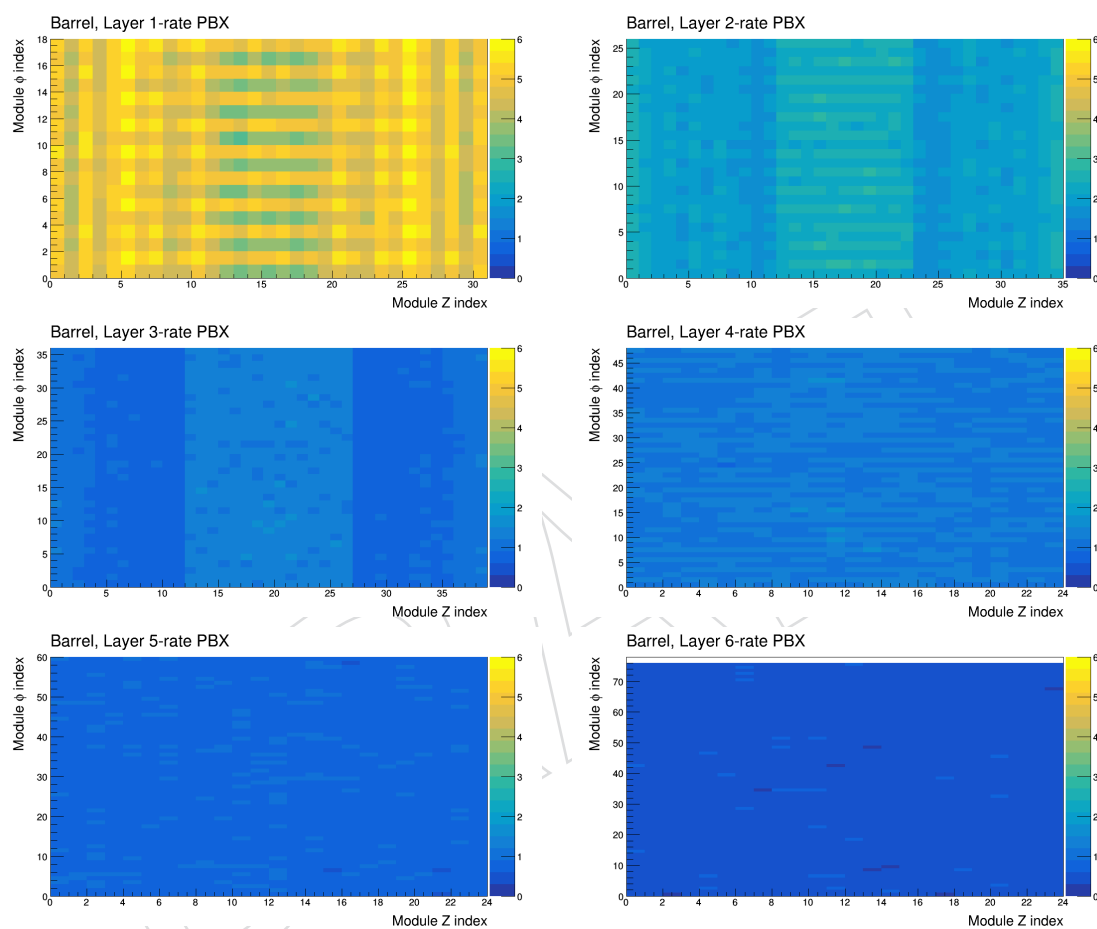


Figure 7: Two dimensional stub rates distributions in barrel layers. Each bin corresponds to a module in z, ϕ position.

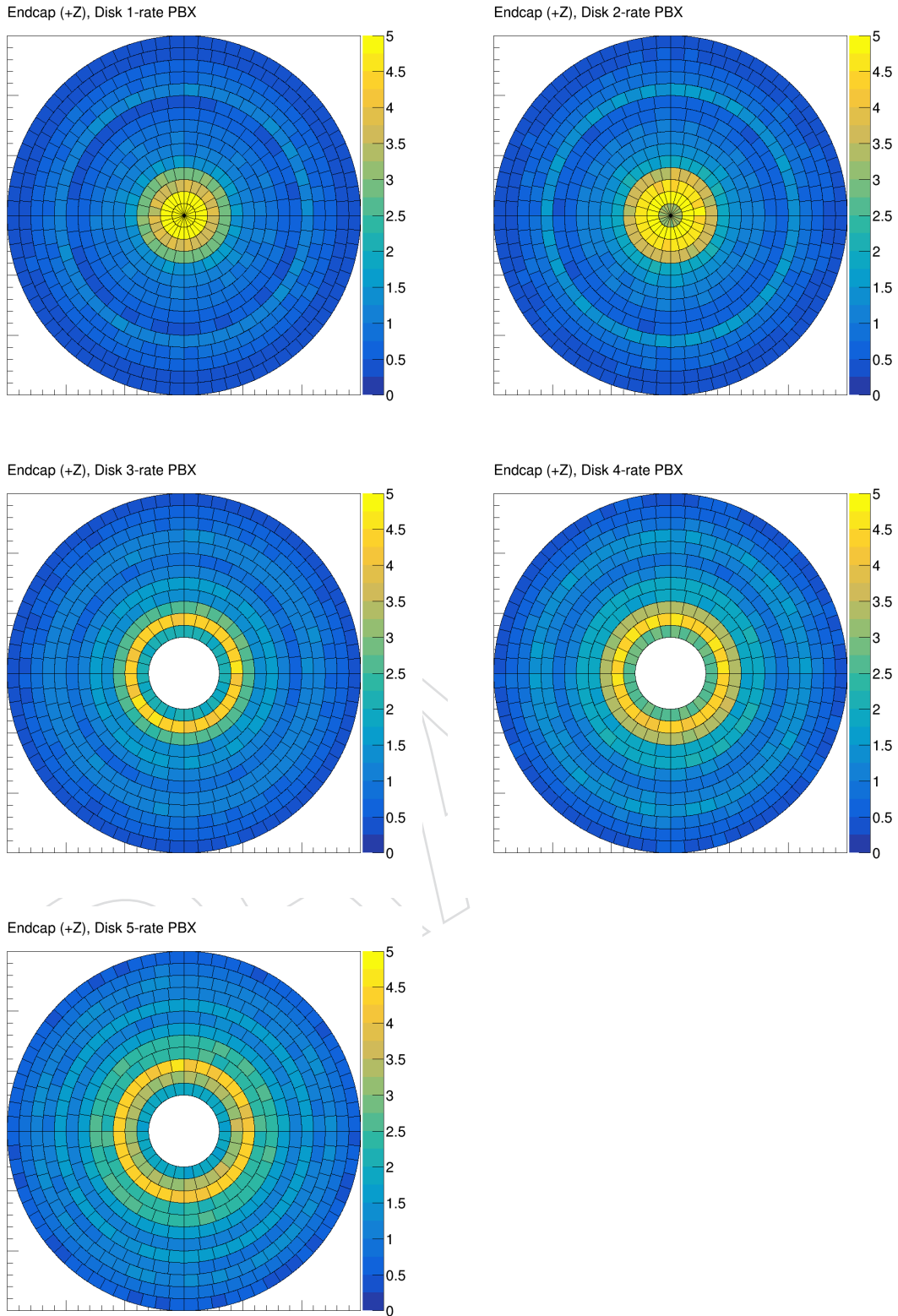


Figure 8: Two dimensional stub rates distributions in endcap disks. Each bin corresponds to a module in r, ϕ position.

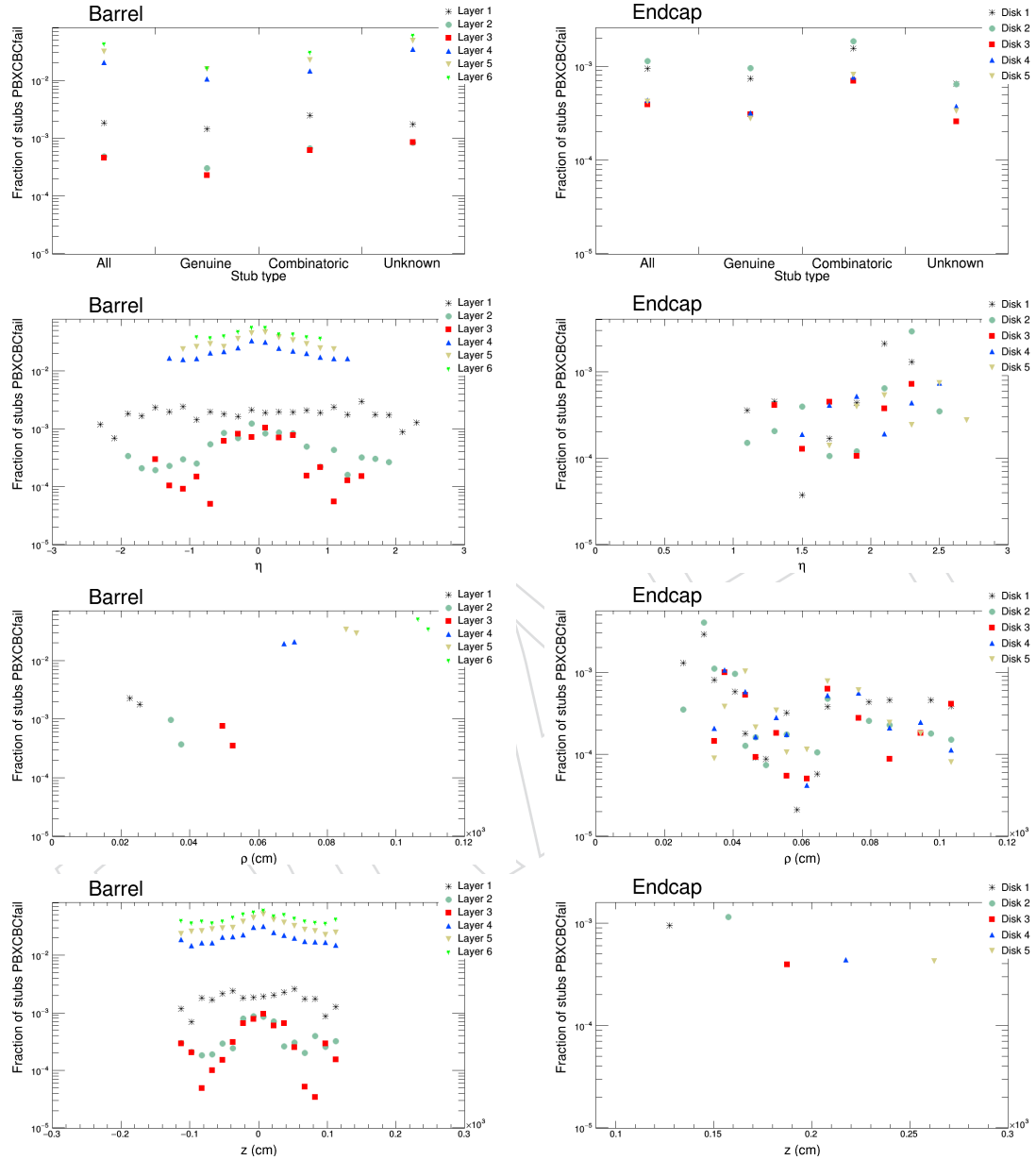


Figure 9: Fraction of stubs that are lost by the CBC/MPA in barrel (left) and endcap (right) are shown as a function of stub types, module η , ρ , and z using $t\bar{t}$ events with 200 PU.

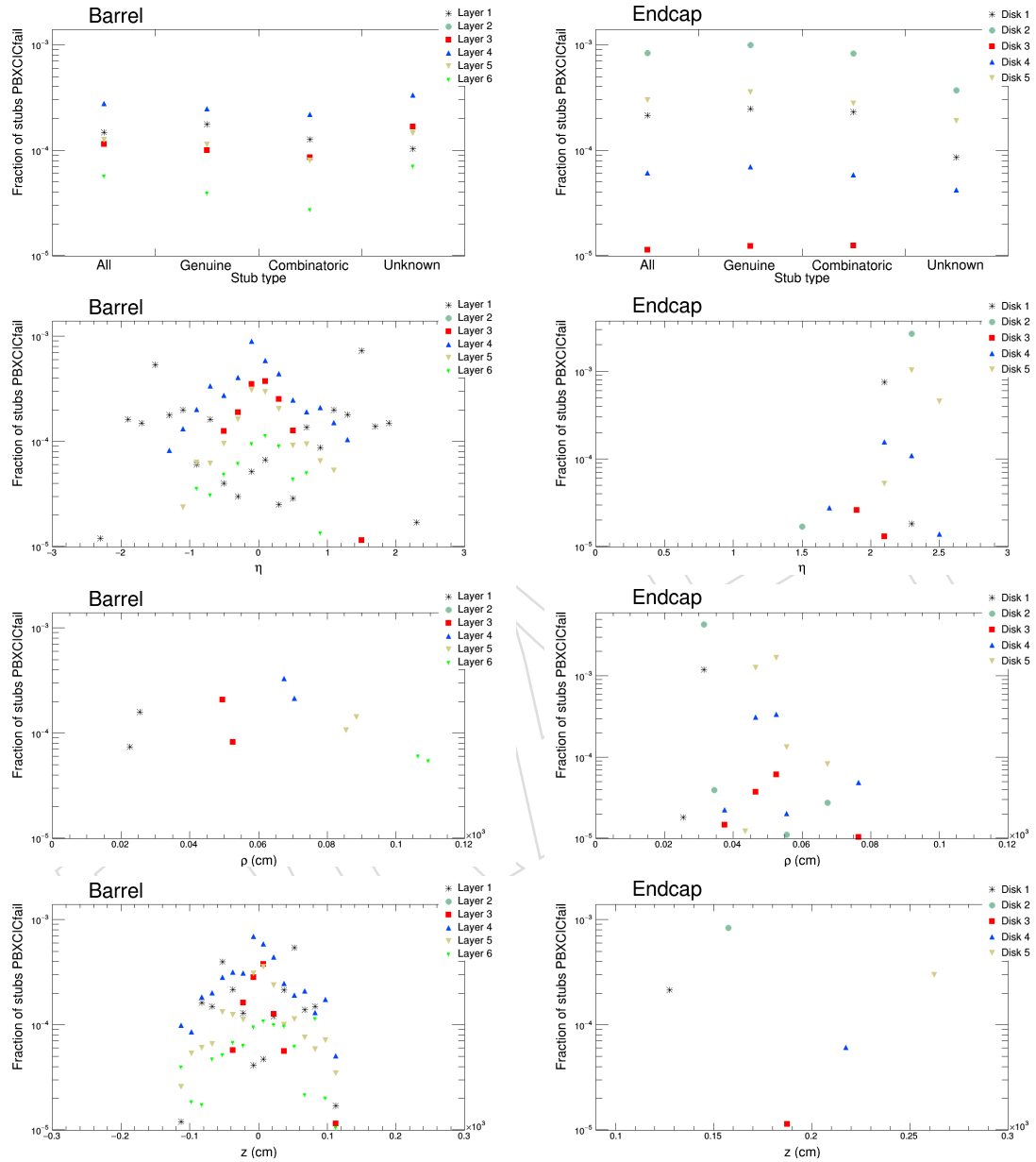


Figure 10: Fraction of stubs that are lost by the CIC in barrel (left) and endcap (right) are shown as a function of stub types, module η , ρ , and z using $t\bar{t}$ events with 200 PU.

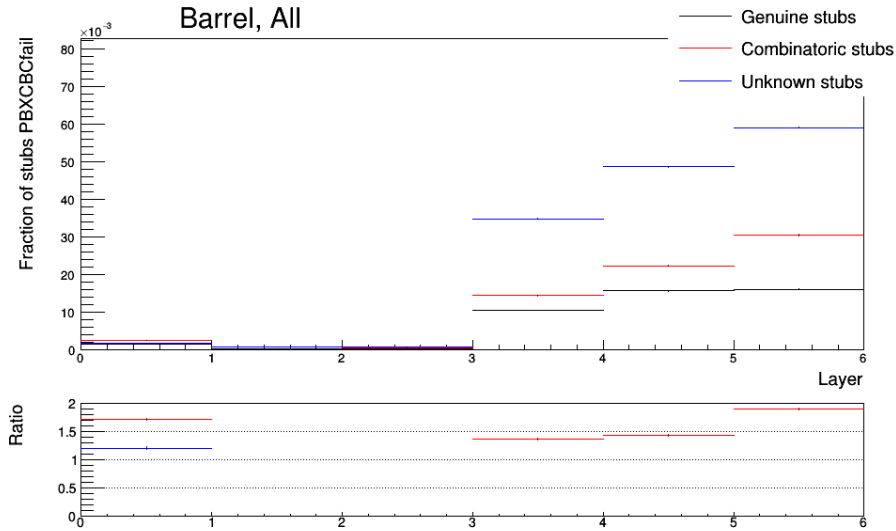


Figure 11: Fraction of stubs that are lost by the CBC/MPAs in barrel are shown for genuine, combinatoric and unknown stubs using $t\bar{t}$ events with 200 PU.

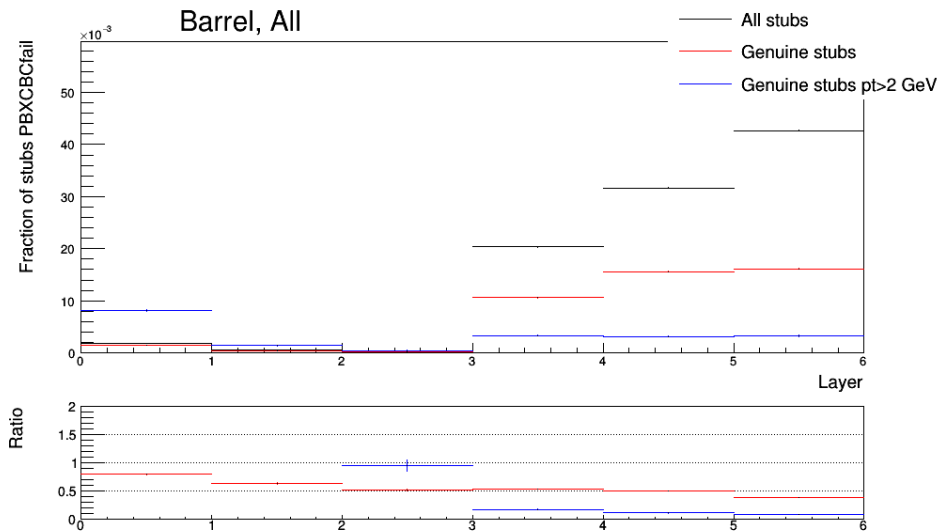


Figure 12: Fraction of stubs that are lost by the CBC/MPAs in barrel are shown for all stubs, genuine stubs and genuine stubs with TP $p_T > 2$ GeV using $t\bar{t}$ events with 200 PU.

129 4 Stub efficiency

130 Stub efficiency, defined as the ratio of the number of genuine clusters (matched to a track) in
131 single track events that are used in a genuine stubs to the number of all genuine clusters.

$$\text{Stub efficiency (1)} = \frac{\text{Number of genuine clusters used in genuine stubs}}{\text{Number of genuine clusters}} \quad (1)$$

132 To measure stub efficiencies for electrons, muons, and displaced muons, we use single lepton
133 samples with zero PU listed in table 1. We loop over TPs in lepton gun sample and find matched
134 clusters for each TP. Then we check if the matched clusters are used in stub construction to find
135 the numerator of the above equation.

In single lepton sample, it is enough to find at least one stub in each layer/Disk. Therefore, we define another stub efficiency;

$$\text{Stub efficiency (2)} = \frac{\text{Number of genuine clusters if a genuine stub is found in a layer/disk}}{\text{Number of genuine clusters}} \quad (2)$$

136 In Figure 13-14, stub reconstruction efficiencies for electron, muon and displaced muon are
137 shown as a function of the TP p_T for the first and second efficiency definition. By construction,
138 the second efficiency is higher than the first efficiency. Similar efficiency plots are shown as a
139 function of the stub η , TP d_0 and TP d_0 in Figures 15-20,

DRAFT

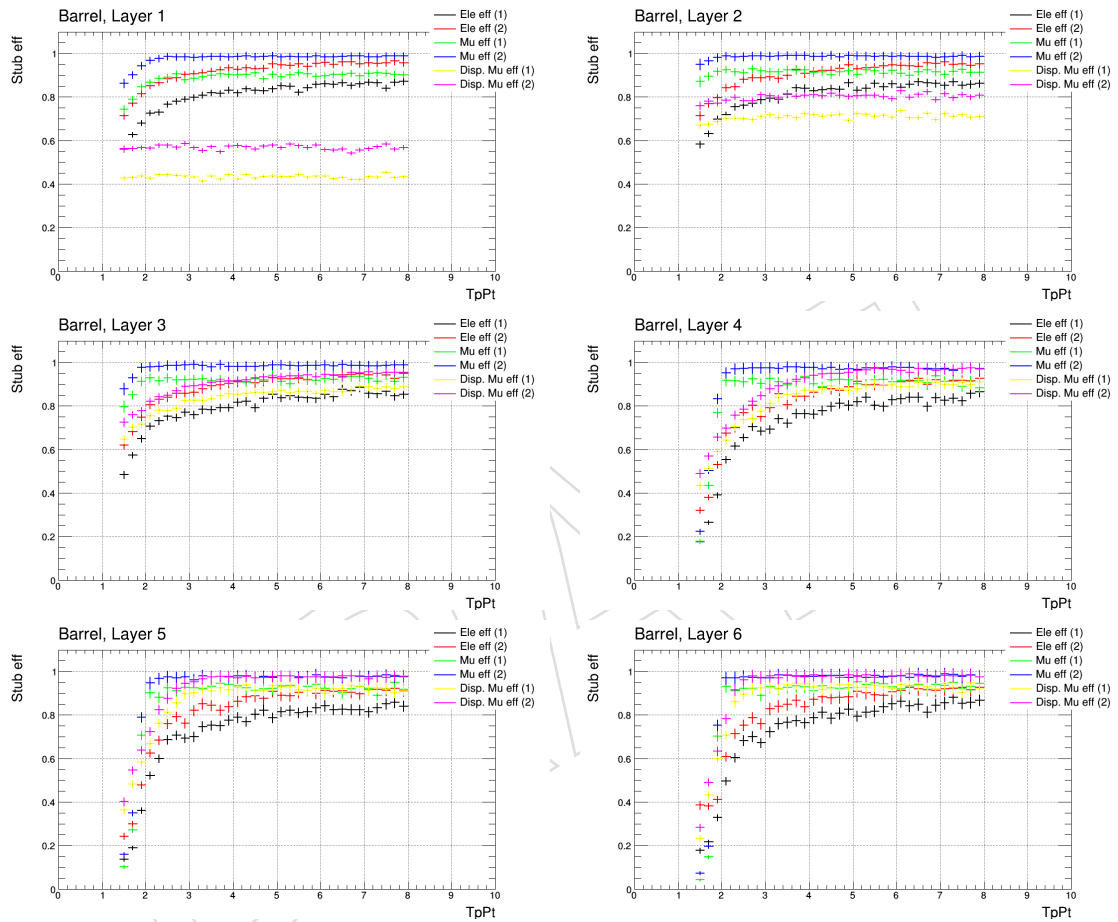


Figure 13: Stub reconstruction efficiencies in barrel layers for electron, muon and displaced muon as a function of TP p_T . Both efficiency definitions defined in the text are shown.

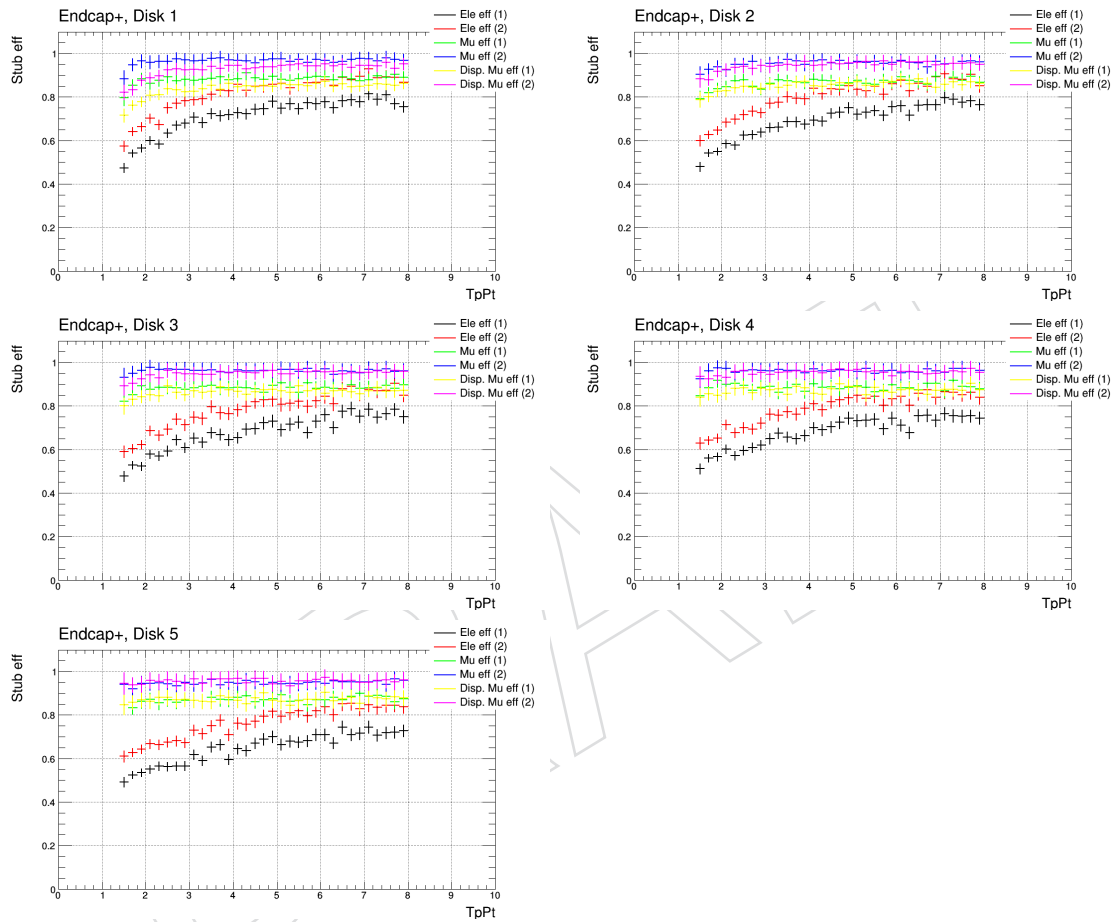


Figure 14: Stub reconstruction efficiencies in endcap disks for electron, muon and displaced muon as a function of TP p_T . Both efficiency definitions defined in the text are shown.

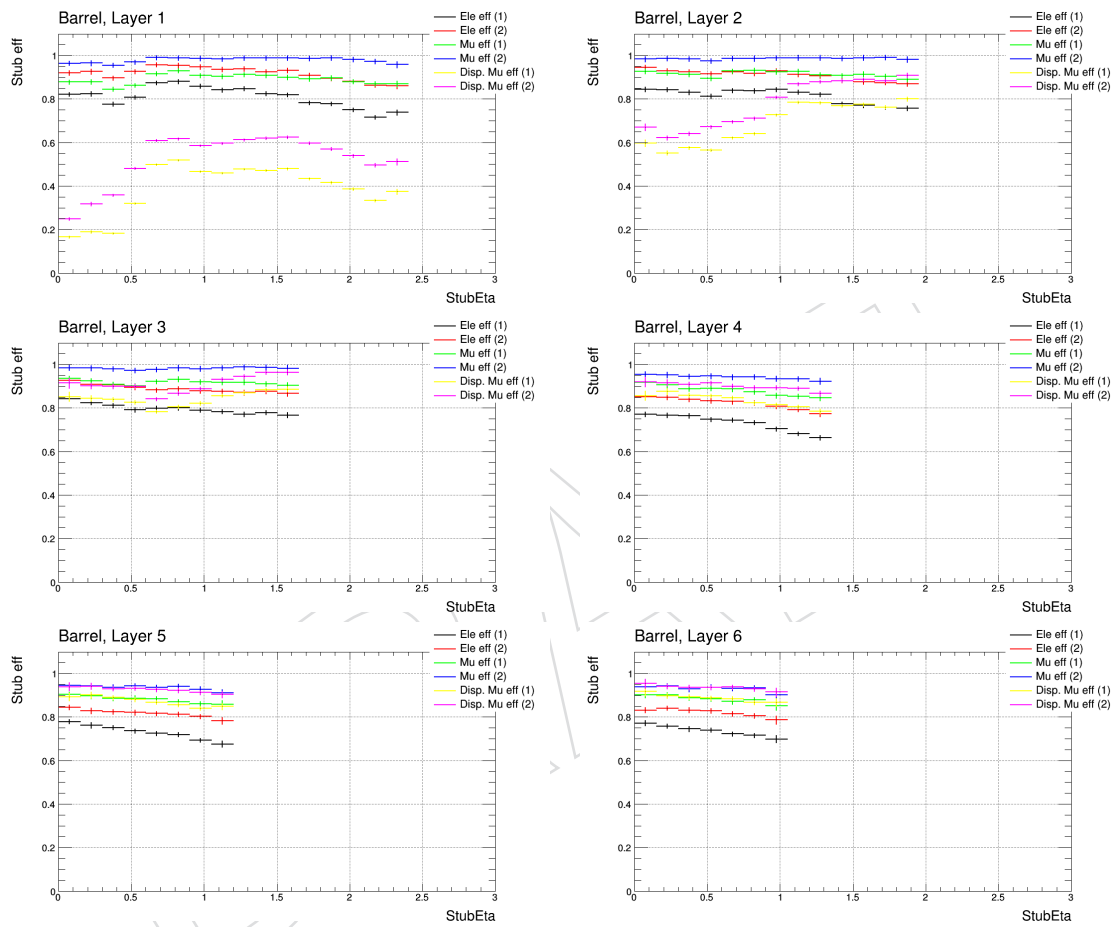


Figure 15: Stub reconstruction efficiencies in barrel layers for electron, muon and displaced muon as a function of Stub Eta. Both efficiency definitions defined in the text are shown.

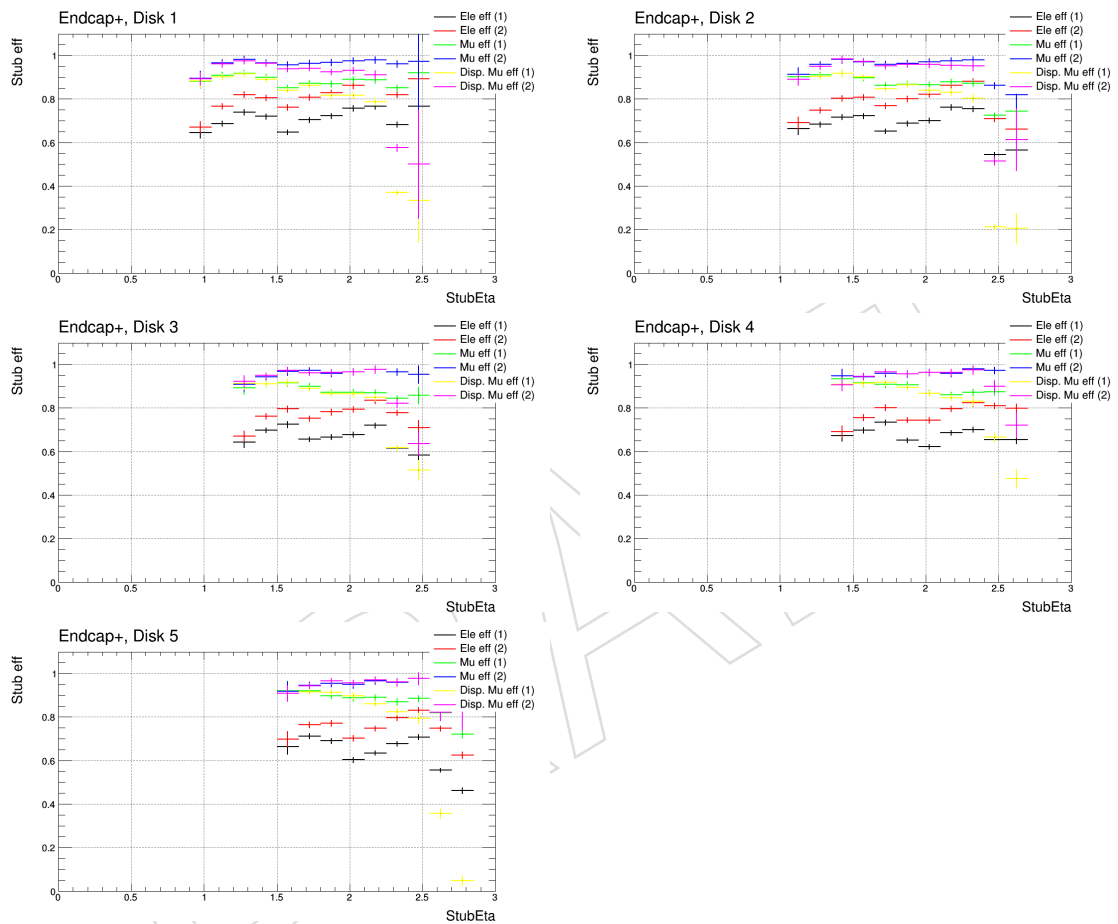


Figure 16: Stub reconstruction efficiencies in endcap disks for electron, muon and displaced muon as a function of Stub Eta. Both efficiency definitions defined in the text are shown.

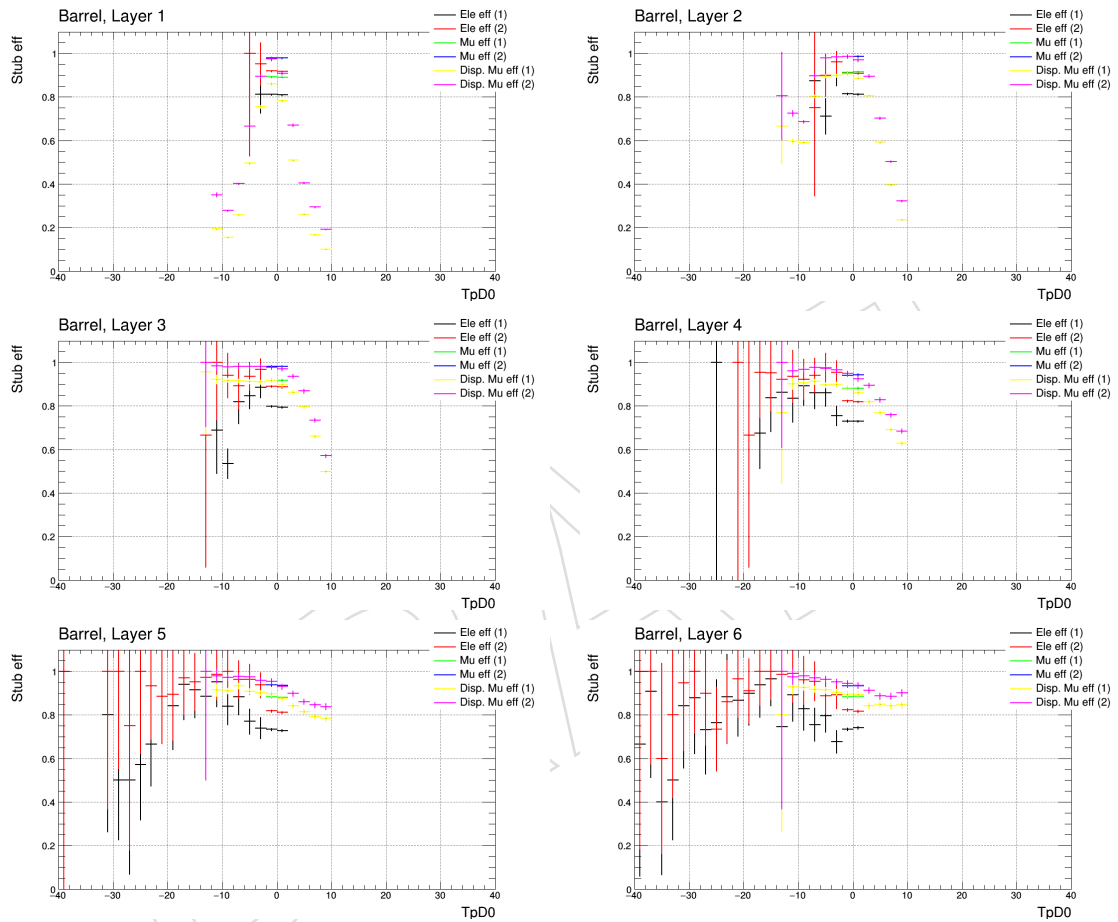


Figure 17: Stub reconstruction efficiencies in barrel layers for electron, muon and displaced muon as a function of TP d_0 . Both efficiency definitions defined in the text are shown.

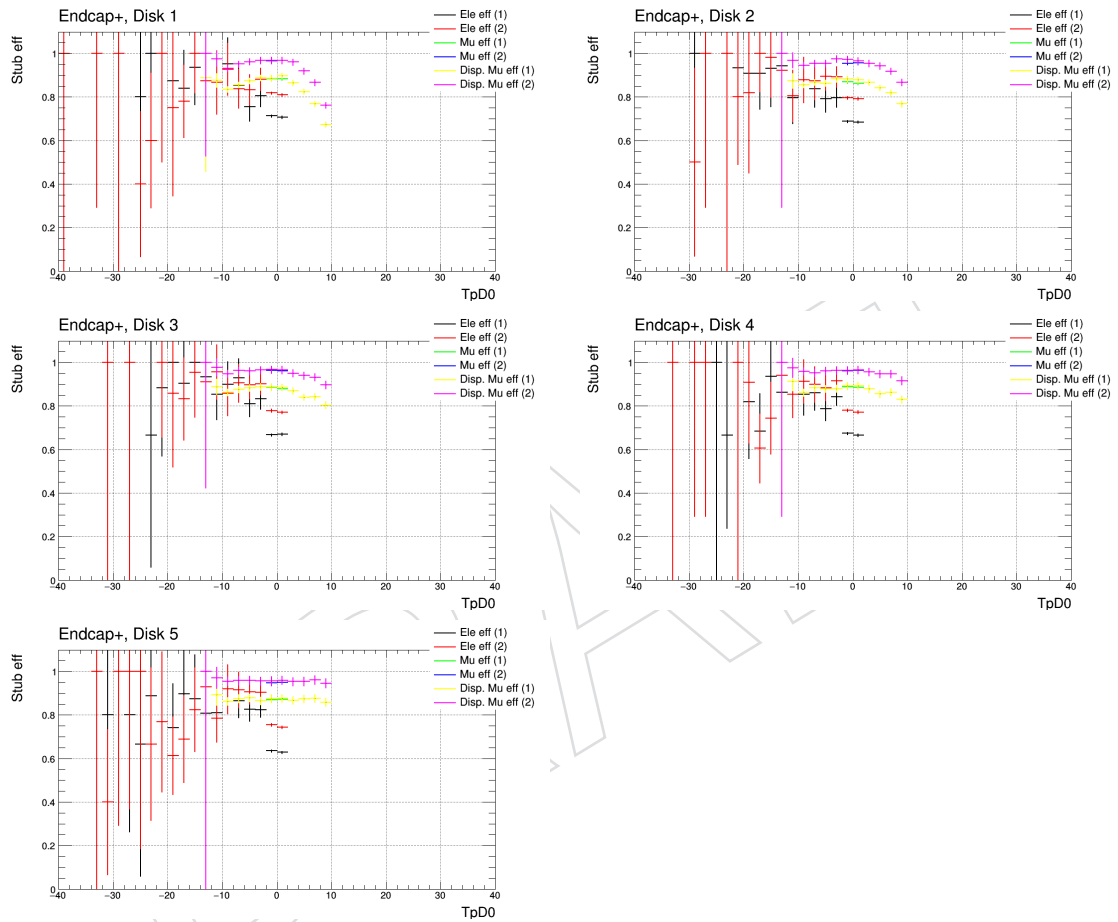


Figure 18: Stub reconstruction efficiencies in endcap disks for electron, muon and displaced muon as a function of TP d_0 . Both efficiency definitions defined in the text are shown.

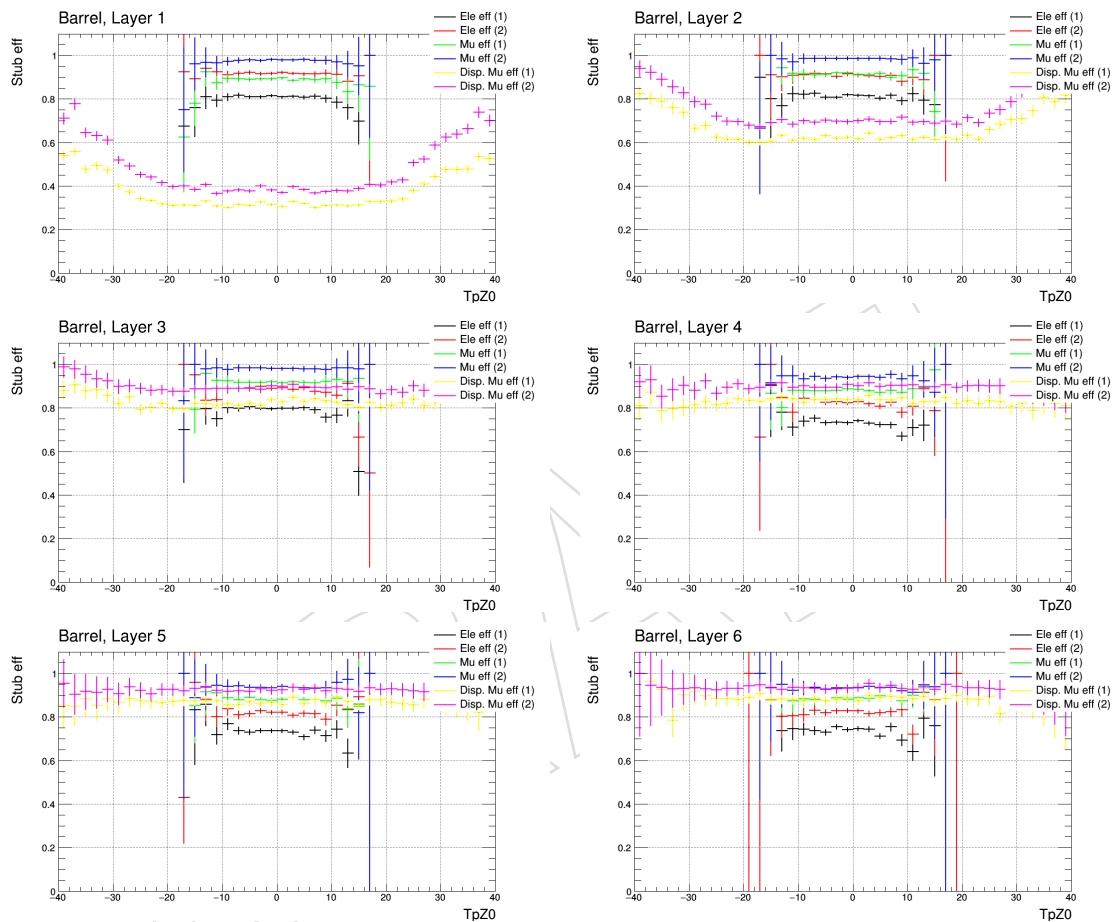


Figure 19: Stub reconstruction efficiencies in barrel layers for electron, muon and displaced muon as a function of TP z_0 . Both efficiency definitions defined in the text are shown.

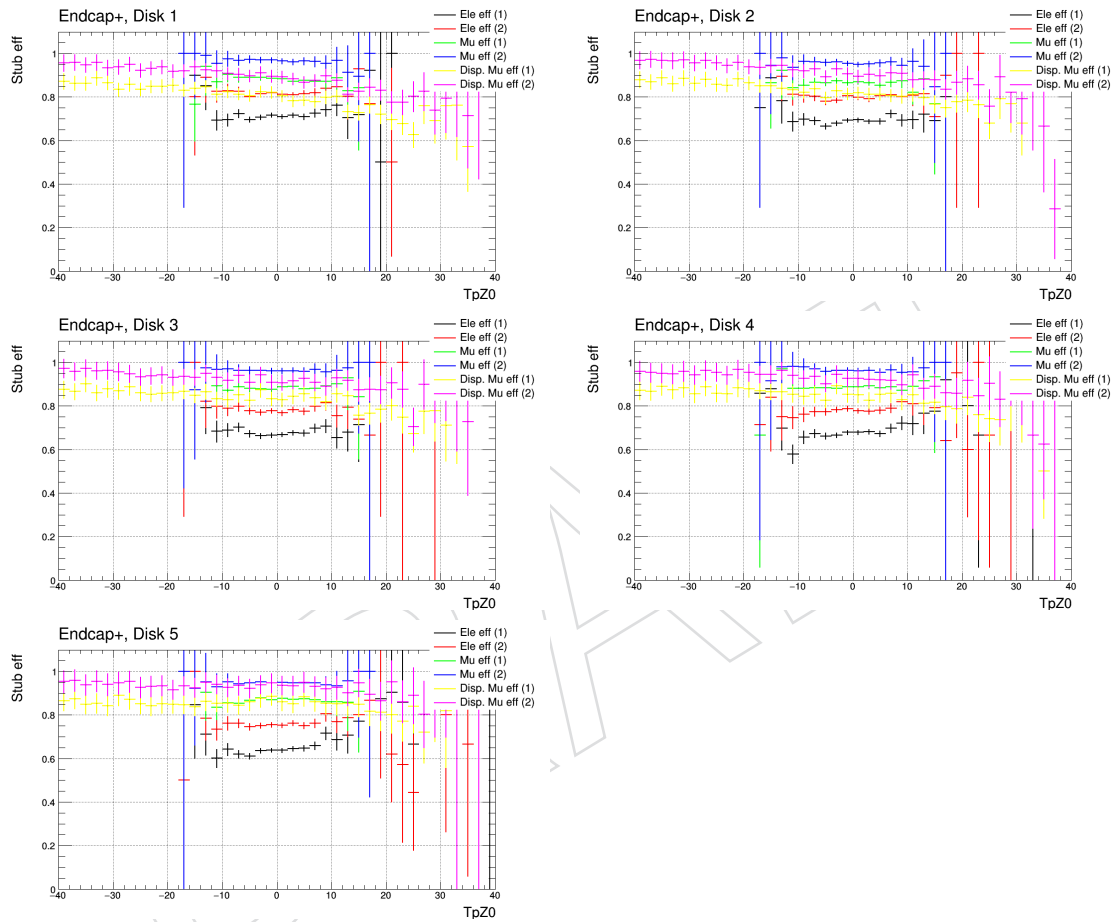


Figure 20: Stub reconstruction efficiencies in endcap disks for electron, muon and displaced muon as a function of TP z_0 . Both efficiency definitions defined in the text are shown.

5 Decoding Bend

The p_T of a track is estimated from the cluster displacement between the top and bottom sensor of a p_T module. This quantity, in units of detector strips, is known as the bend. The bend can be approximated from track parameters with

$$bend = \Delta r \frac{r}{2p} rinv = \Delta r \frac{1.14qr}{2p_T}$$

Where r is the radial position of the hit, p is the strip pitch, $rinv$ is the inverse radius of curvature of the track, q is the charge. Δr is the radial separation of the hits in a p_T module given by:

$$\Delta r = \frac{s}{\sin(\alpha) \frac{z}{r} + \cos(\alpha)} ; \alpha_{flat} = 0^\circ, \alpha_{disk} = 90^\circ$$

The bend, measured in half-strip bins, is encoded into 3 or 4 bits (PS/2S) which represent the range of bends accepted for that module. In general the bend bins are merged starting with high bend or low p_T bins. This loss of resolution only occurs for modules with stub window size larger than 1.5/3.5 (PS/2S). To use the encoded bend for a set of modules we define a map from encoded bend to some bend parameter, which is then used to estimate p_T . This map is what we call the bend decoding.

The stub-to-stub or stub-to-track bend correlations are quickly assessed via the use of pre-computed lookup tables (LUT) that are indexed by stub positions and encoded bends. Hardware constraints limit the granularity of lookup table bins, in particular this means that any single r/z bin in the disks and PS layers may contain several modules for which the same encoded bend represents different values of p_T . The bend decoding must account for this variation for optimal performance. The bend decoding for some region is constructed by considering all modules and their bends which map to the encoded bend. Using this we can construct a range in our bend parameter that covers the variation of all the modules in that LUT region.

In the legacy algorithm the bend decoding is defined using simulated events. This was estimated by optimizing the efficiency in single muon events and then adjusting the rate in some areas with $ttbar+200PU$ events. This method does not require knowledge of module tilt, window sizes, or encoding scheme. The drawback is that in general any change to the bend window sizes, encoding scheme, bend parameter, or LUT r/z bins requires the user to redefine the bend decoding. Here we introduce a process for which the bend decoding can be calculated as a function of the stub window sizes and LUT r/z bins. These changes can enable future studies involving alternative bend parameters, LUT r/z bins, or encoding schemes.

In practice the bend is decoded in terms of a quantity called bendstrip which is proportional to the inverse radius of curvature ($rinv$) and is inversely proportional to p_T . The bendstrip is calculated from track parameters using:

$$bendstrip = 0.18 \frac{r}{2} rinv$$

Where 0.18 represents the sensor spacing for the 2S modules and r is the radial position of the stub. This bend parameter works well for the PS/2S layers due to a single layer varying only a little in r however this introduces issues when decoding the bend in the disks. The mean bendstrip for a particular encoded bend, depends on the radial position of the stub as shown in



Figure 21: Representation of the encoding and proposed decoding algorithm for three rings in layer 1. Each row shows the encoding of a specific ring and their lengths represent the range in bendstrip that is covered by their stub window size. The half integer numbers are the possible (positive) bends, and the colors represent their mapping to the encoded bend. The green dashed lines represent the decoded bend for an encoded bend of 2. The encoded bend is a representation of the detector bend in 3 bits, an encoded bend of 2 does not correspond to a detector bend of 2. The bend cut is a tunable parameter.

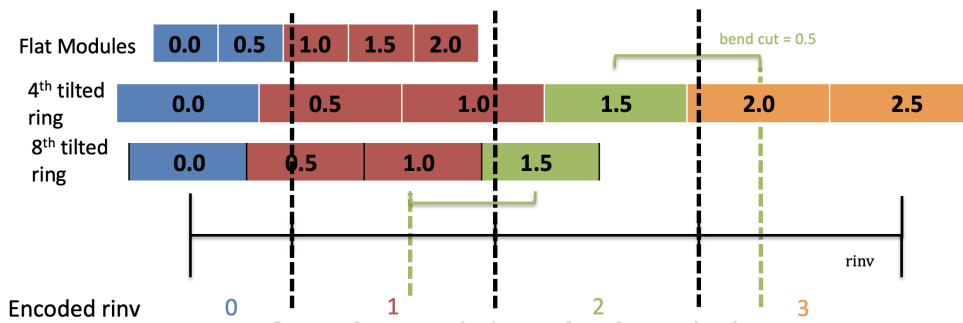


Figure 22: Representation of a potential rinv encoding/decoding algorithm for three rings in layer 1. Each row shows the encoding of a specific ring and their lengths represent the range in rinv that is covered by their stub window size. The half integer numbers are the possible (positive) bends, and the colors represent their mapping to the encoded rinv. The black dashed lines are the rinv bins, the green dashed lines represent the decoded rinv for an encoded rinv of 2.

173 figure 23 . To account for this additional r bins were added to the lookup tables used during the
 174 track seeding stage (TrackletEngine). It may be beneficial to also add additional r bins to the
 175 lookup tables in the track-to-stub association stage (MatchEngine). A different choice of bend
 176 parameter (rinv) or encoding scheme may also fix this issue.

177 This improvement to the bend decoding process is enabled in part by the use of module infor-
 178 mation obtained with the SensorModule class implemented in L1Trigger/TrackTrigger. With-
 179 out the module information (position, tilt, stub window size) we would not be able to properly
 180 represent a modules bend in whatever bend parameter space we are using. To get this informa-
 181 tion where we need it we are required to pass the Setup class (L1Trigger/TrackTrigger) through
 182 to the TrackletLUT. In the TrackletLUT we define new methods which are used to decode the
 183 bend in LUT creation.

184 The bend decoding process uses the methods getSensorModules, getBendCut, and sometimes,
 185 getTanRange which are defined in the TrackletLUT class. To decode the bend we first find a set
 186 of all modules for which we want the decoding to be valid. This is done using the getSensor-
 187 Modules method. There are two ways that this method is used in the track trigger code. The

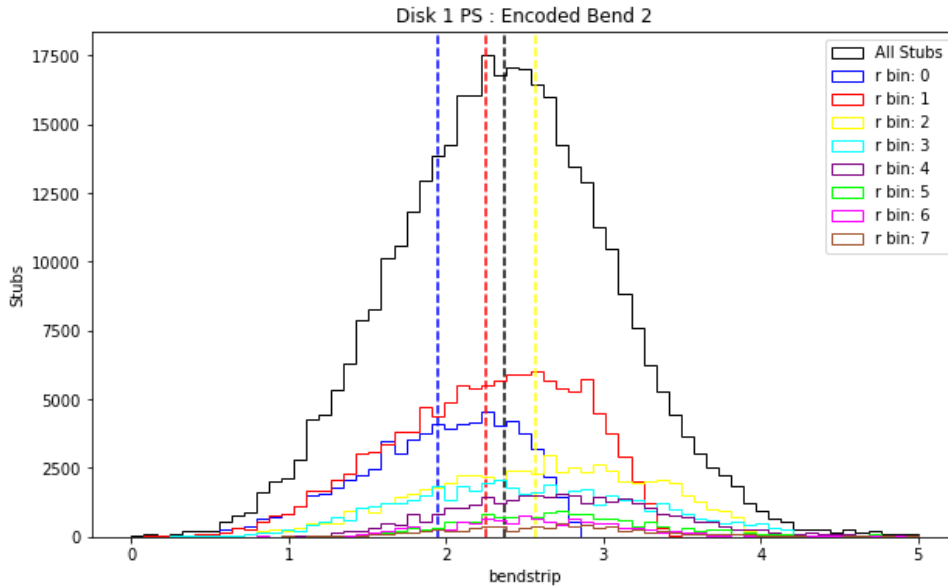


Figure 23: The dashed lines represent the mean bendstrip for an ensemble of stubs, with an encoded bend of 2, in a particular r-bin of disk 1 (PS). This shows that the bendstrip for a particular encoded bend varies as a function of r in the disks. To recover bend resolution one can either bin the disks in r or use a bend parameter which is independent of r . These stubs are taken from a sample of 5000 TTbar 200PU events.

188 default is to return all modules, unique in $|z|$ for a given layer/disk and module type (PS/2S);
 189 this is used mostly in the MatchEngine. For the TrackletEngine lookup tables we can reduce
 190 the number of modules by passing the `getSensorModules` method a range in $\tan(\theta)$ that will
 191 cover only the relevant modules. Theta here is measured with respect to the radial axis. To
 192 account for displaced tracks the max/min $\tan(\theta)$ are measured from ± 15 cm along the z axis.

193 Once we find our sensor modules we pass that information to the `getBendCut` method. To
 194 start we initialize a few data structures to store our bend decoding information and then loop
 195 over all the sensor modules. For each module we loop over all possible bend values, which are
 196 determined by the stub window size. For each bend in a given module we find its encoded
 197 bend value and calculate the corresponding bend max/min, defined as the bend plus/minus
 198 a bend cut. Finally we transform the bend max/min into the chosen bend parameter space,
 199 bendstrip in this case, and update the bend decoding to cover this range for this particular
 200 encoded bend value. This process provides a different bend decoding for every r/z bin in the
 201 Tracklet/MatchEngine lookup tables.

202 The bend cuts are used to balance the rates of real (true positive) and fake (false positive) stub
 203 combinations or track projections, while keeping the total pass rate below the threshold set by
 204 truncation. A real combination will pass in the LUT and also has matching tracking particles,
 205 while a fake combination will pass in the LUT but not have any matching tracking particles.
 206 Bend cuts which are too small will miss too many real tracks while bend cuts which are too
 207 large will lead to real tracks being truncated. The tuning strategy used here is just to match the
 208 true positive rate of the legacy algorithm. In general this method of decoding the bend results
 209 in a lower false positive and therefore truncation rate while maintaining or improving the true
 210 positive rate for the samples studied.

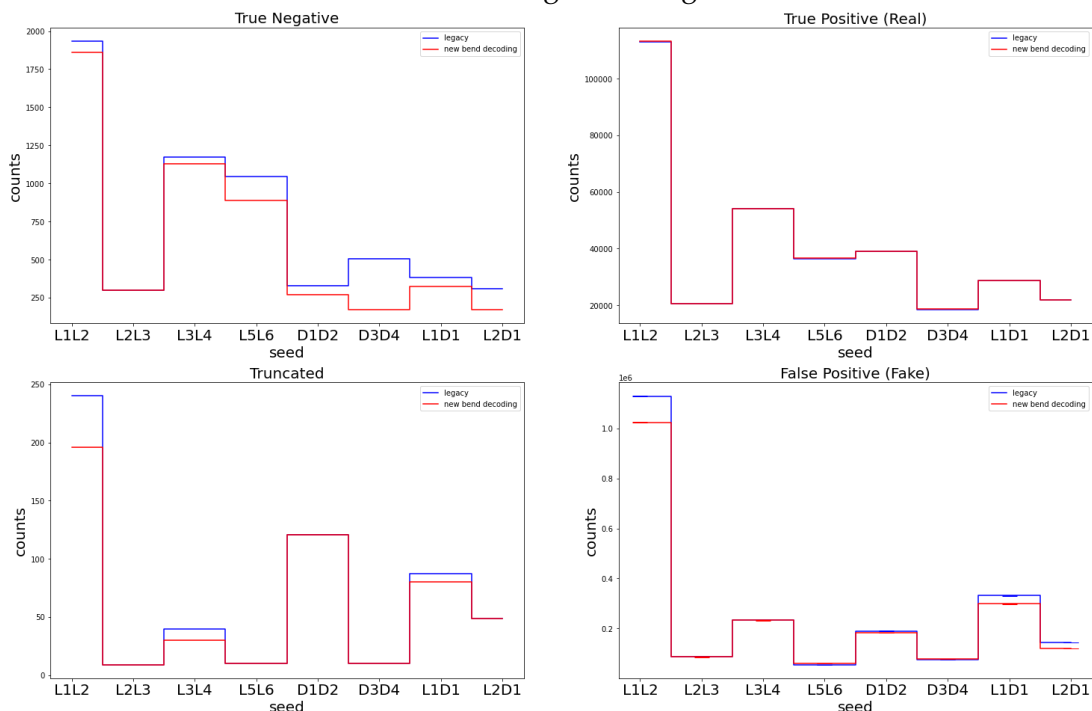
211 The bend cuts, defined in `TrackFindingTracklet/Interface/Settings.h`, are represented as multi-
 212 ples of the approximate bend resolution:

$$\sigma_{bend} \approx \frac{1}{\sqrt{6}} [5]$$

213 For the TrackletEngine the bend cuts are all between 2-2.6; the MatchEngine however requires
214 bend cuts up to 4 to maintain efficiency because the disks are not binned in r. The true negative,
215 true positive, truncation, and false positive rates are compared in figure 24.

DRAFT

TrackletEngine Tuning



MatchEngine Tuning

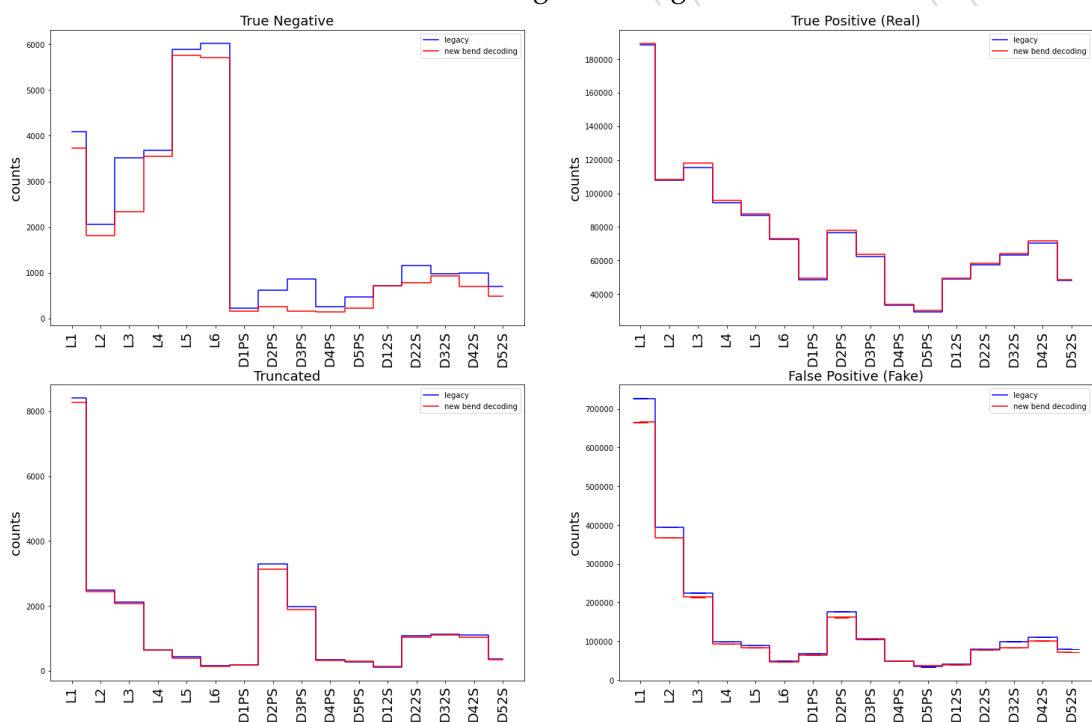


Figure 24: TrackletEngine (top) and MatchEngine (bottom) tuning. The Tracklet/MatchEngine associate stubs using their bend information. A “True” association is one in which all stubs share a matching tracking particle. A positive association is one that passes their respective LUT. The bend cuts are set such that the True Positive (Real) rate is larger than the legacy algorithm (equivalently a smaller True Negative rate). The bend cuts are parameterized by seed in the TrackletEngine and by layer/disk in the MatchEngine. These plots are made using 500 TTbar 200PU events.

6 Stub window tuning

Stubs are reconstructed by the CBC and MPA chips each time two correlated clusters will be found in the two layers (see Figure 2). Stub rates and reconstruction efficiencies depend on the stub acceptance window size. Establishing this window size, known as stub window (SW), in all the tracker regions is a fundamental step requiring a careful optimization. Indeed, small stub windows will ensure very good data reduction with a cost in efficiency, whereas large stub windows will provide good efficiency with a cost in rate [5].

As the signal information is binary, a group of adjacent hits is considered a cluster. The cluster width w is defined as the number of strips in the cluster

$$w = n_{last} - n_{first} + 1 \quad (3)$$

Where n_{first} and n_{last} are the indices of the first and last strips in the cluster, respectively, in accordance with the geometric order of the strips on the sensors. The cluster position X is defined as the mean value

$$X = \frac{n_{last} + n_{first}}{2} \quad (4)$$

The cluster width is given in steps of full-strips, while the position is in half-strips.

The stub position μ is defined as the mean cluster position per module

$$\mu = \frac{X_{top} + X_{bottom}}{2} \quad (5)$$

Where X_{top} and X_{bottom} are the cluster positions in the top and bottom sensor of the module, respectively. The stub window ΔX is defined as the difference between the cluster positions in the top and bottom sensor,

$$\Delta X = X_{top} - X_{bottom} \quad (6)$$

the stub window size is given in steps of half-strips, while the stub position is in quarter-strips. This window size varies from as little as two strips in the PS modules at the lowest radii in the forward region to nine strips in the current version of SW tune [5]. For the 2S modules the acceptance window varies between 6-15 strips. These acceptance windows are configurable and can be tuned to manage the rate for the trigger data [6].

The latest SW tune which is used in simulated samples are called "tight tune" which is optimized to ensure a good efficiency for muon stubs. There is another tune called "loose tune" in which electron efficiencies are also included (see https://indico.cern.ch/event/681577/contributions/2816628/attachments/1572998/2482715/UpgradeSim_111217.pdf). Stub windows should vary in different geometrical regions of the tracker to control rates and FE losses. In the current tune, SW is defined for 108 geometrical regions as are listed bellow and are shown in Figure 25;

- Flat modules in barrel layers (6 regions)
- Tilted modules in the first three layers ($3 \times 12 = 36$ regions)
- Rings in the first two disks ($2 \times 15 = 30$ regions)
- Rings in the last three disks ($3 \times 12 = 36$ regions)

In order to update the stub tune, we need to know the following variables in 108 geometrical regions of the tracker

- Stub rate as a function of stub window size

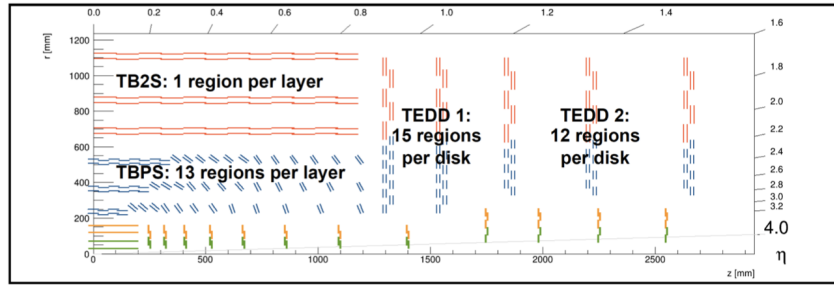


Figure 25: Tracker regions requiring a specific SW tuning. TB2S: Tracker Barrel with 2S modules. TBPS: Tracker Barrel with PS modules. TEDD: Tracker Endcap Double Disks [5].

- 243 • FE losses as a function of stub window size
- 244 • Stub efficiency for electron, muon as a function of stub window size

245 As was discussed in the previous sections, we use $t\bar{t}$ events with PU=200 for finding the stub-
 246 rate/FE-losses and single lepton samples for measuring the stub reconstruction efficiencies.
 247 For SW tuning, we find efficiencies for muon in [2,8] GeV and electron in [4,8] GeV p_T range to
 248 be in the plateau of the efficiency turn on curve. We run the same chain of stub reconstruction
 249 using a fix value for the SW size in all 108 geometrical regions and measure the above variables.
 250 In the following, the input SW sizes for 108 geometrical regions of the tracker are printed for
 251 tight and loose tunes (see L1Trigger/TrackTrigger/python/TTStubAlgorithmRegister_cfi.py).

```

252 # PU200 tight tuning, optimized for muons
253 BarrelCut = cms.vdouble( 0, 2, 2.5, 3.5, 4.5, 5.5, 7),
254 TiltedBarrelCutSet = cms.VPSet(
255   cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
256   cms.PSet( TiltedCut = cms.vdouble( 0, 3, 3, 2.5, 3, 3, 2.5, 2.5, 2, 1.5, 1.5, 1, 1 ) ),
257   cms.PSet( TiltedCut = cms.vdouble( 0, 3.5, 3, 3, 3, 3, 2.5, 2.5, 3, 3, 2.5, 2.5, 2.5 ) ),
258   cms.PSet( TiltedCut = cms.vdouble( 0, 4, 4, 4, 3.5, 3.5, 3.5, 3.5, 3, 3, 3, 3, 3 ) ),
259 ),
260 EndcapCutSet = cms.VPSet(
261   cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
262   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 2.5, 2.5, 3, 2.5, 3, 3.5, 4, 4, 4.5, 3.5, 4, 4.5, 5, 5.5 ) ),
263   cms.PSet( EndcapCut = cms.vdouble( 0, 0.5, 2.5, 2.5, 3, 2.5, 3, 3, 3.5, 3.5, 4, 3.5, 3.5, 4, 4.5, 5 ) ),
264   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 3, 3, 2.5, 3.5, 3.5, 3.5, 4, 3.5, 3.5, 4, 4.5 ) ),
265   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 2.5, 3, 2.5, 3.5, 3, 3, 3.5, 3.5, 3.5, 4, 4 ) ),
266   cms.PSet( EndcapCut = cms.vdouble( 0, 0.5, 1.5, 3, 2.5, 3.5, 3, 3, 3.5, 4, 3.5, 4, 3.5 ) ),
267 )

268 # PU200 loose tuning, optimized for robustness
269 BarrelCut = cms.vdouble( 0, 2.0, 3, 4.5, 6, 6.5, 7.0),
270 TiltedBarrelCutSet = cms.VPSet(
271   cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
272   cms.PSet( TiltedCut = cms.vdouble( 0, 3, 3, 2.5, 3, 3, 2.5, 2.5, 2, 1.5, 1.5, 1, 1 ) ),
273   cms.PSet( TiltedCut = cms.vdouble( 0, 4, 4, 4, 4, 4, 4.5, 5, 4, 3.5, 3.5, 3 ) ),
274   cms.PSet( TiltedCut = cms.vdouble( 0, 5, 5, 5, 5, 5, 5.5, 5, 5, 5.5, 5.5, 5.5 ) ),
275 ),
276 EndcapCutSet = cms.VPSet(
277   cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
278   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 2.5, 2.5, 3.5, 5.5, 5.5, 6, 6.5, 6.5, 6.5, 6.5, 6.5, 6.5, 7, 7 ) ),
279   cms.PSet( EndcapCut = cms.vdouble( 0, 0.5, 2.5, 2.5, 3, 5, 6, 6, 6.5, 6.5, 6.5, 6.5, 6.5, 6.5, 7, 7 ) ),
280   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 3, 4.5, 6, 6.5, 6.5, 6.5, 7, 7, 7, 7 ) ),
281   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 2.5, 3.5, 6, 6.5, 6.5, 6.5, 6.5, 7, 7, 7 ) ),
282   cms.PSet( EndcapCut = cms.vdouble( 0, 0.5, 1.5, 3, 4.5, 6.5, 6.5, 7, 7, 7, 7, 7 ) ),
283 )

```

284 We have calculated stub rates, FE losses, and stub efficiencies for the following fix SWs; 0.5, 1.0,
 285 1.5, 2.0, 2.5, 3.0, 3.5, 4.0, 4.5, 5.0, 5.5, 6.0, 6.5, 7.0. For example,

```

286 #Fixed tune
287 BarrelCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1),
288 TiltedBarrelCutSet = cms.VPSet(
289   cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
290   cms.PSet( TiltedCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
291   cms.PSet( TiltedCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
292   cms.PSet( TiltedCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
293 ),
294 EndcapCutSet = cms.VPSet(
295   cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
296   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
297   cms.PSet( EndcapCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),

```

```

298     cms.PSet ( EndcapCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
299     cms.PSet ( EndcapCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
300     cms.PSet ( EndcapCut = cms.vdouble( 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 ) ),
301 )

```

302 The following algorithm is used to choose the optimum window size with high-efficiency and
 303 low-rate for each geometrical region:

- 304 • The CBC/MPA stub fail fraction should be less than 1%
- 305 • The CIC stub fail fraction should be less than 0.5%
- 306 • Normalize the stub reconstruction efficiencies for electron and muon to the efficiency
 307 obtained with the largest possible window size (7.0)
- 308 • The normalized stub reconstruction efficiencies for electron and muon should be
 309 greater than 60%
- 310 • Choose the smallest window size where the efficiencies of the electron or muon do
 311 not increase more than 0.005 with respect to the closest larger window size

312 The stub window tune which is optimized based on the stub reconstruction efficiency for muon
 313 (muon + electron) is called “New tight” (“New loose”). New tunes are;

```

314 # New tight tune based on simulated events CMSSW_11_3_0_pre3, D76
315 BarrelCut = cms.vdouble(0, 2.0, 2.0, 3.0, 4.5, 5.5, 6.5),
316 TiltedBarrelCutSet = cms.VPSet(
317     cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
318     cms.PSet( TiltedCut = cms.vdouble( 0, 2.0, 2.0, 2.0, 2.5, 2.0, 2.0, 2.0, 1.5, 1.5, 1.5, 1.0, 1.0 ) ),
319     cms.PSet( TiltedCut = cms.vdouble( 0, 2.5, 2.5, 2.5, 2.5, 2.0, 2.0, 2.0, 2.5, 2.5, 2.0, 2.0, 2.0 ) ),
320     cms.PSet( TiltedCut = cms.vdouble(0, 3.5, 3.5, 3.0, 3.0, 3.0, 3.0, 2.5, 2.5, 2.5, 2.5, 2.5, 2.0 ) ),
321 ),
322 EndcapCutSet = cms.VPSet(
323     cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
324     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.5, 2.5, 3.0, 3.0, 4.0, 2.5, 3.0, 3.5, 4.0, 5.0 ) ),
325     cms.PSet( EndcapCut = cms.vdouble(0, 0.5, 1.5, 1.5, 2.0, 2.0, 2.0, 2.5, 2.5, 3.0, 3.5, 2.0, 2.5, 3.0, 4.0, 4.0 ) ),
326     cms.PSet( EndcapCut = cms.vdouble(0, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 2.5, 3.5, 2.0, 2.5, 3.5, 3.5 ) ),
327     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 3.0, 2.0, 2.0, 3.0, 3.0 ) ),
328     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 3.0, 2.0, 2.0, 2.5 ) ),
329 )
330 )
331 \

332 # New loose tune based on simulated events CMSSW_11_3_0_pre3, D76
333 BarrelCut = cms.vdouble(0, 2.0, 3.0, 4.0, 5.0, 7.0, 7.0),
334 TiltedBarrelCutSet = cms.VPSet(
335     cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
336     cms.PSet( TiltedCut = cms.vdouble( 0, 3.0, 2.0, 2.0, 3.0, 2.5, 3.0, 2.0, 1.5, 1.5, 1.5, 1.0, 1.0 ) ),
337     cms.PSet( TiltedCut = cms.vdouble( 0, 4.0, 3.5, 3.5, 3.5, 4.0, 4.0, 3.5, 5.0, 4.5, 4.0, 4.5, 3.0 ) ),
338     cms.PSet( TiltedCut = cms.vdouble(0, 5.0, 5.0, 5.0, 4.0, 4.0, 4.0, 4.0, 4.0, 5.0, 6.0, 5.0, 5.5 ) ),
339 ),
340 EndcapCutSet = cms.VPSet(
341     cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
342     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 2.5, 5.0, 3.0, 4.5, 6.0, 6.0, 6.0, 6.0, 7.0, 6.0, 7.0, 6.0, 7.0, 7.0 ) ),
343     cms.PSet( EndcapCut = cms.vdouble(0, 0.5, 2.5, 4.0, 5.0, 5.0, 4.0, 4.0, 6.0, 6.0, 7.0, 5.5, 6.0, 5.5, 6.5, 7.0 ) ),
344     cms.PSet( EndcapCut = cms.vdouble(0, 3.5, 5.5, 6.5, 4.5, 6.0, 6.5, 7.0, 7.0, 4.5, 7.0, 7.0, 7.0 ) ),
345     cms.PSet( EndcapCut = cms.vdouble(0, 2.0, 5.5, 6.0, 6.0, 6.0, 6.5, 6.0, 7.0, 7.0, 6.0, 7.0, 7.0 ) ),
346     cms.PSet( EndcapCut = cms.vdouble(0, 1.5, 4.5, 5.5, 5.0, 7.0, 7.0, 6.0, 7.0, 7.0, 7.0, 7.0, 7.0 ) ),
347 )
348 )
349 \

```

350 In figures 26-36, rates, CBC/MPA fail fractions, CIC fail fractions, normalized muon and elec-
 351 tron efficiencies are shown in the barrel layers and endcap disks for above tunes. In figures 37-
 352 40, nominal stub reconstruction efficiencies (not normalized) for muon and electron are shown.
 353 Each region of the mentioned 108 geometrical regions of the tracker are shown as an independ-
 354 ent bin in x-axis. We have also divided the flat barrel part, although they are counted as one
 355 region in stub tuning procedure. In the barrel histograms, first bin is related to the leftmost
 356 module and last bin is related to the rightmost module in z-axis. In the endcap histograms,
 357 first bin is related to the innermost ring and last bin is related to the outermost ring in r-axis.

358 In table 2, the total number of stubs are shown for the four available tunes. As it is clear from
 359 the last column of the table 2, the new tight tune leads to around 20% less stubs in the first

360 three layers in the barrel compared to the tight tune. Moreover, the stub rate reduction is more
 361 significant in the endcap disks (around 30% in all disks).

Table 2: Stub rate for the tight, loose, new tight, and new loose tunes

Barrel layer	Tight tune	loose Tune	New tight tune	New loose tune	new tight / tight
1	2.66e+03	2.66e+03	2.35e+03	2.55e+03	0.884
2	1.9e+03	2.62e+03	1.49e+03	2.72e+03	0.784
3	1.46e+03	2.16e+03	1.22e+03	1.91e+03	0.839
4	1.37e+03	1.78e+03	1.37e+03	1.51e+03	1.0
5	1.14e+03	1.31e+03	1.14e+03	1.39e+03	1.0
6	8.02e+02	8.02e+02	7.54e+02	8.01e+02	0.94
Endcap disks					
1	8.32e+02	1.18e+03	6.03e+02	1.19e+03	0.724
2	9.21e+02	1.38e+03	6.35e+02	1.4e+03	0.689
3	6.89e+02	1.19e+03	5.16e+02	1.36e+03	0.75
4	8.14e+02	1.42e+03	5.31e+02	1.64e+03	0.652
5	8.74e+02	1.51e+03	6.37e+02	1.89e+03	0.729

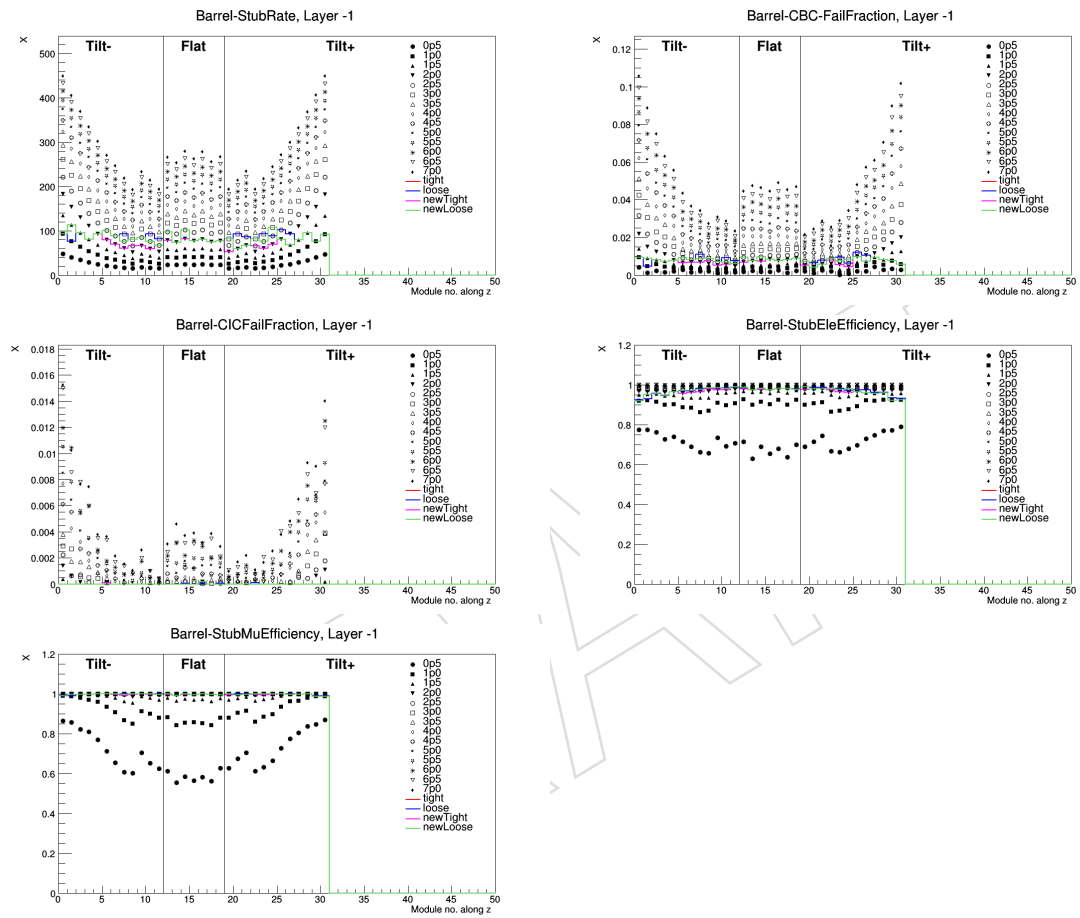


Figure 26: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 1.

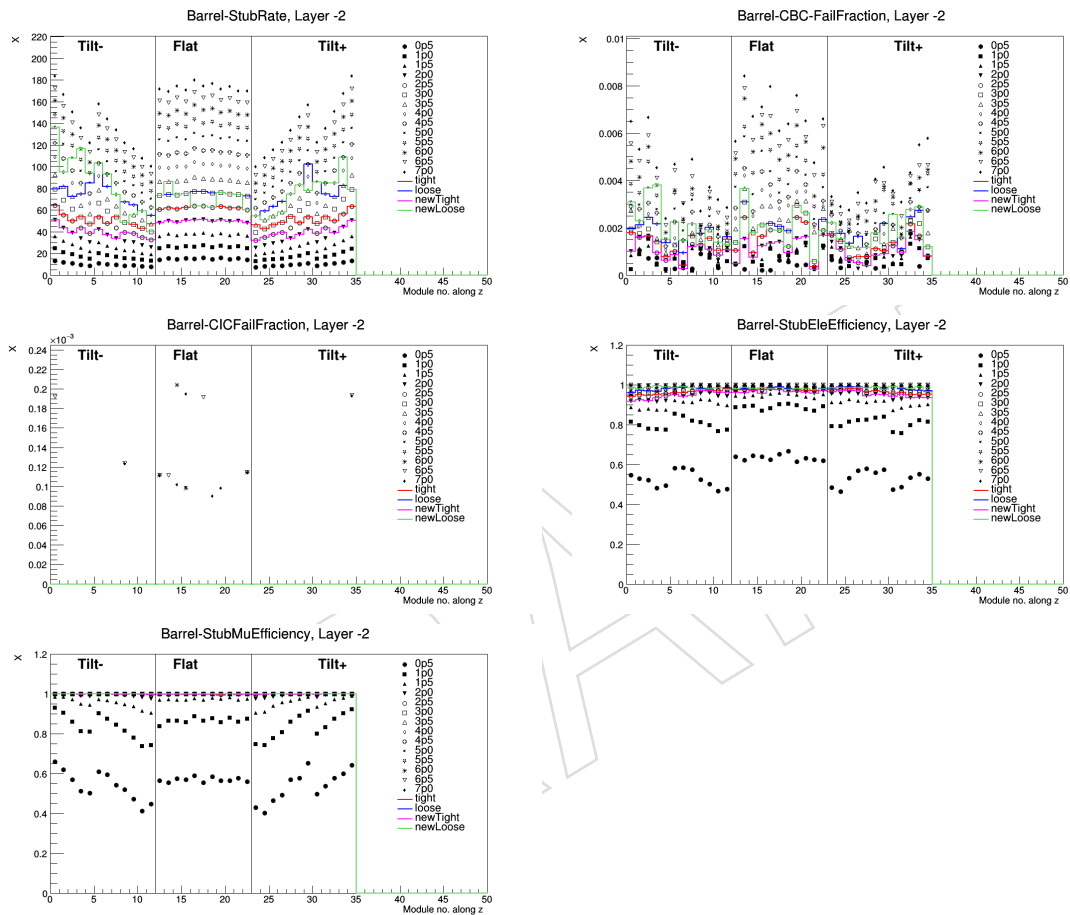


Figure 27: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 2.

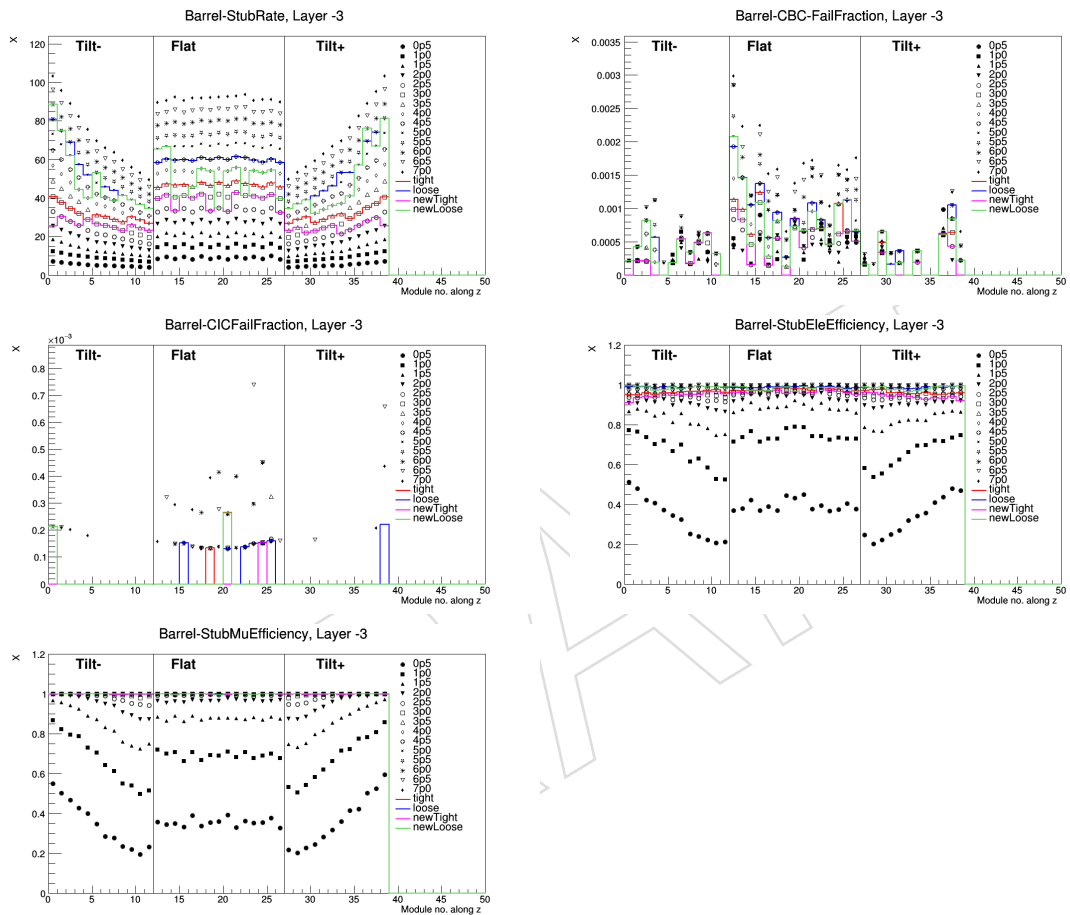


Figure 28: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 3.

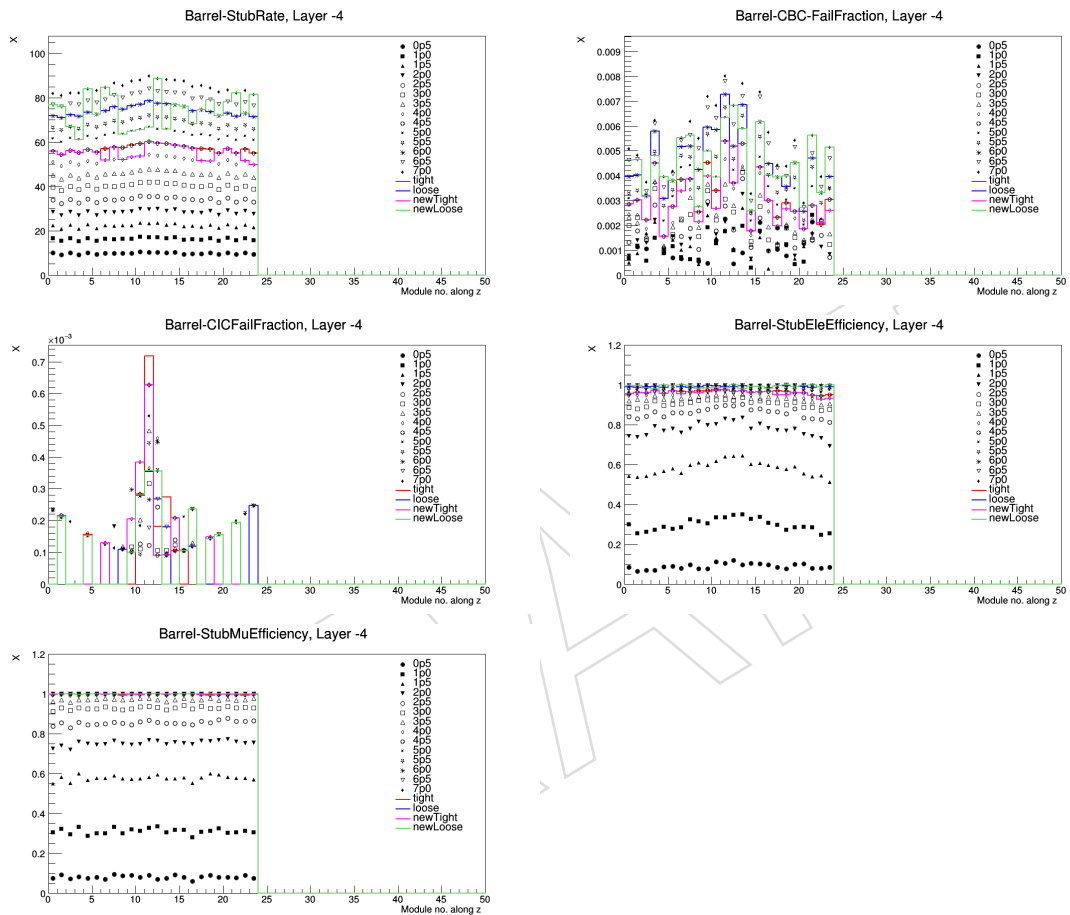


Figure 29: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 4.

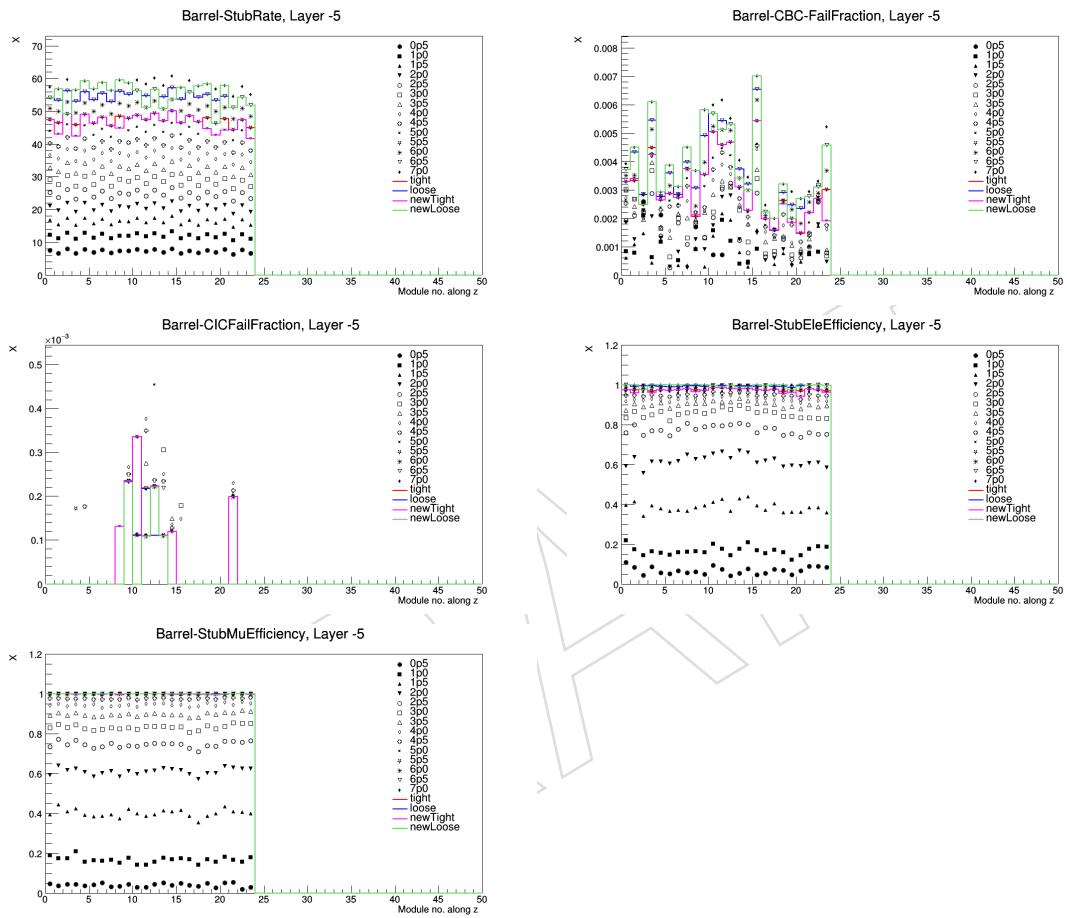


Figure 30: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 5.

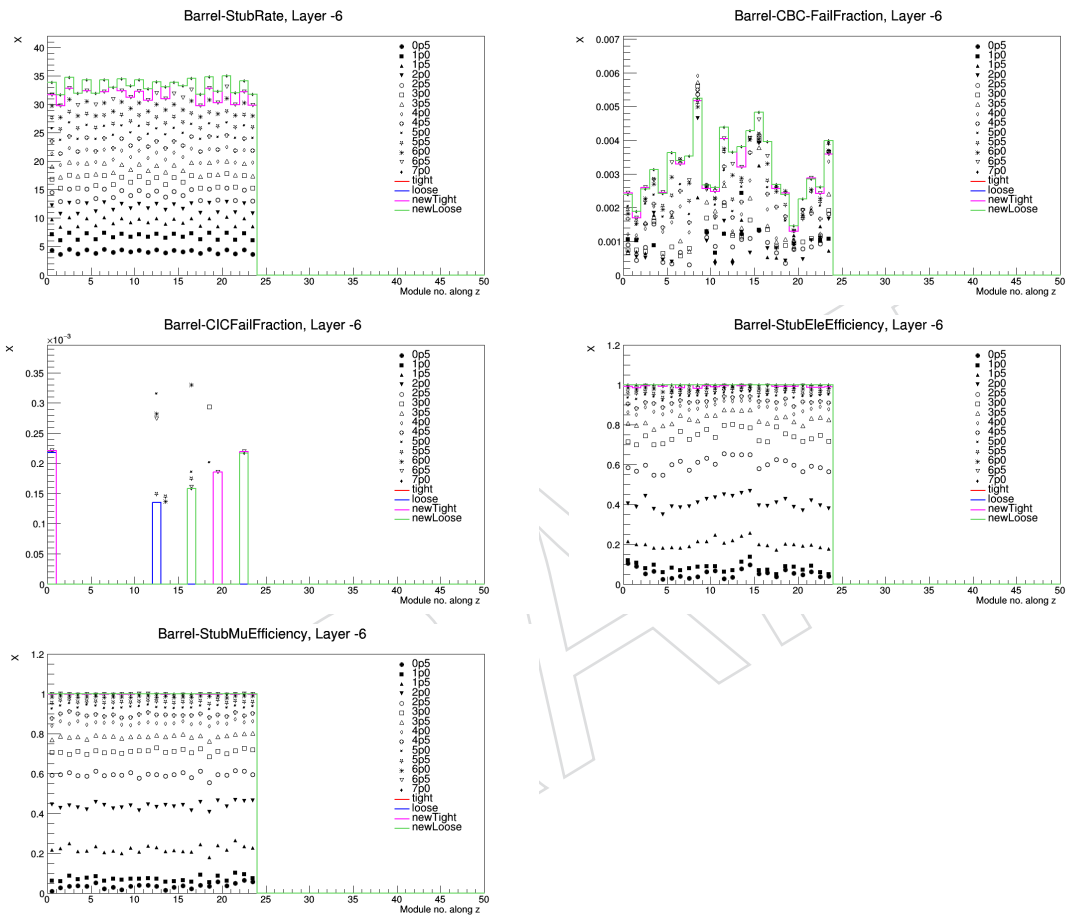


Figure 31: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in barrel layer 6.

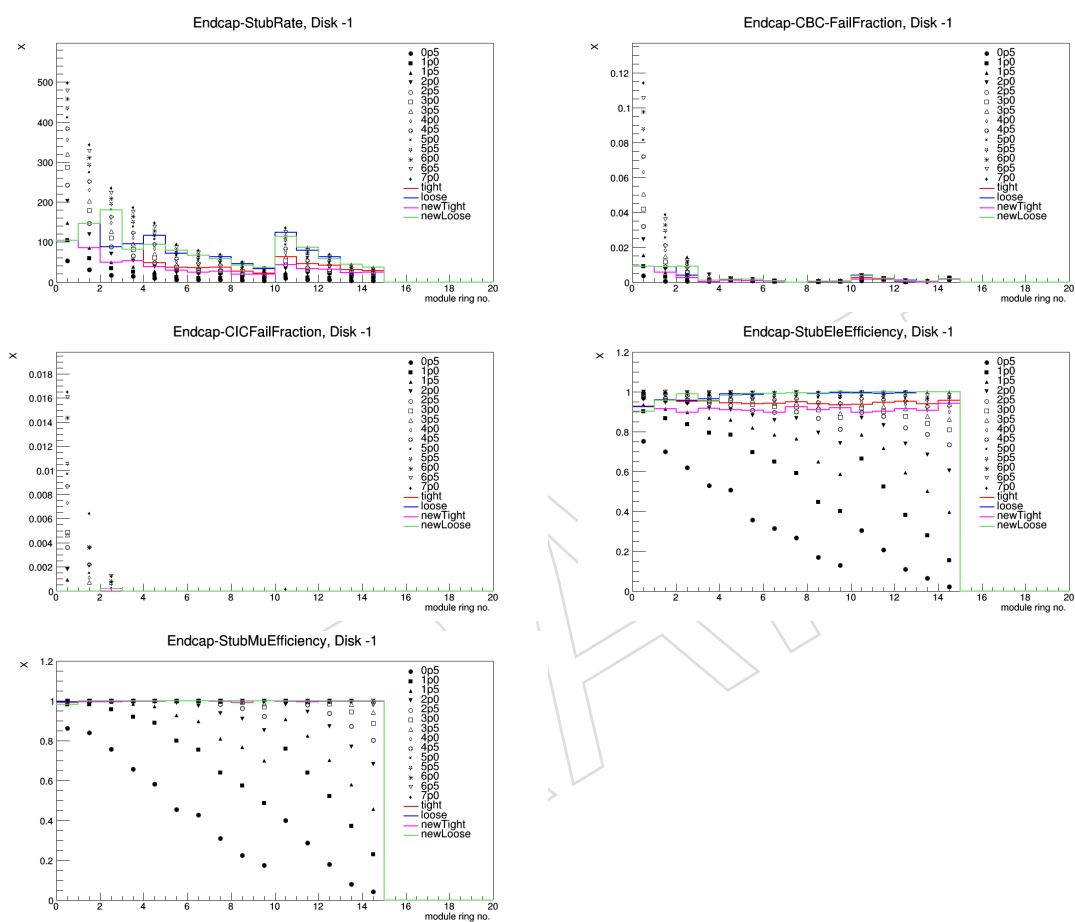


Figure 32: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in endcap disk 1.

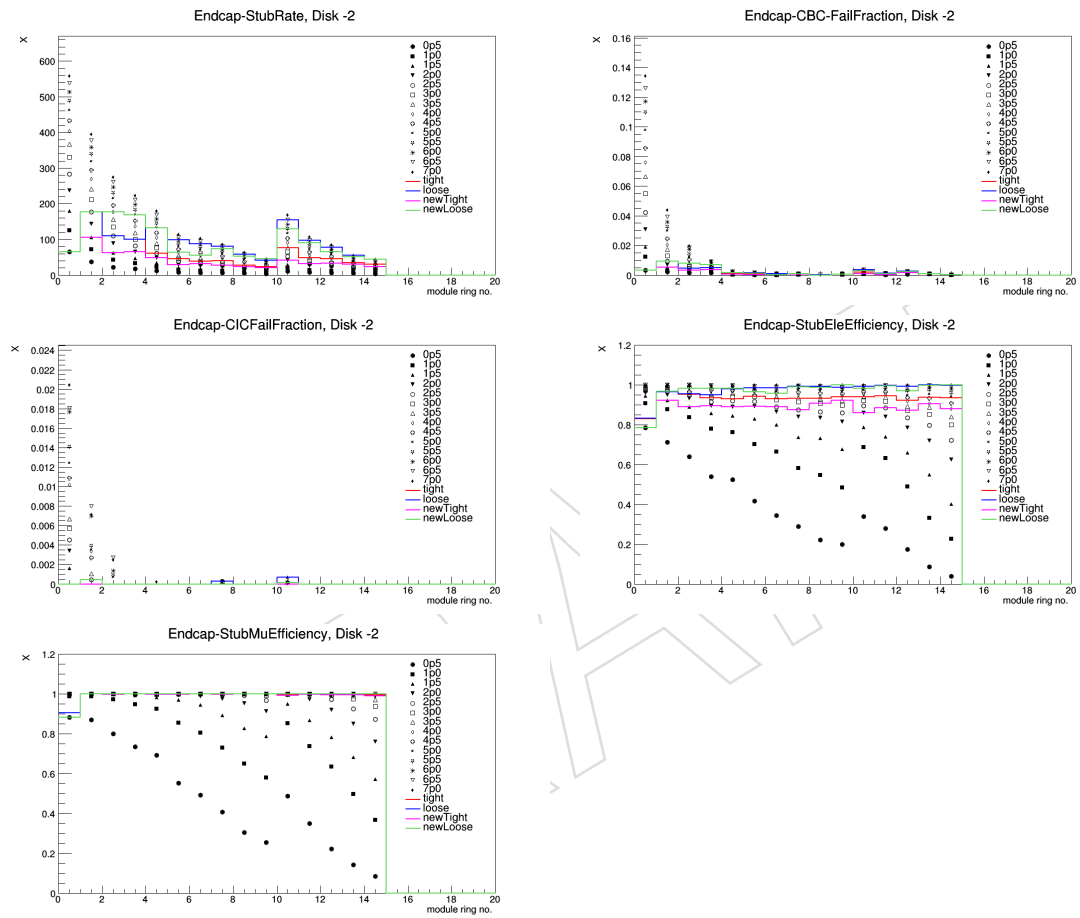


Figure 33: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in endcap disk 2.

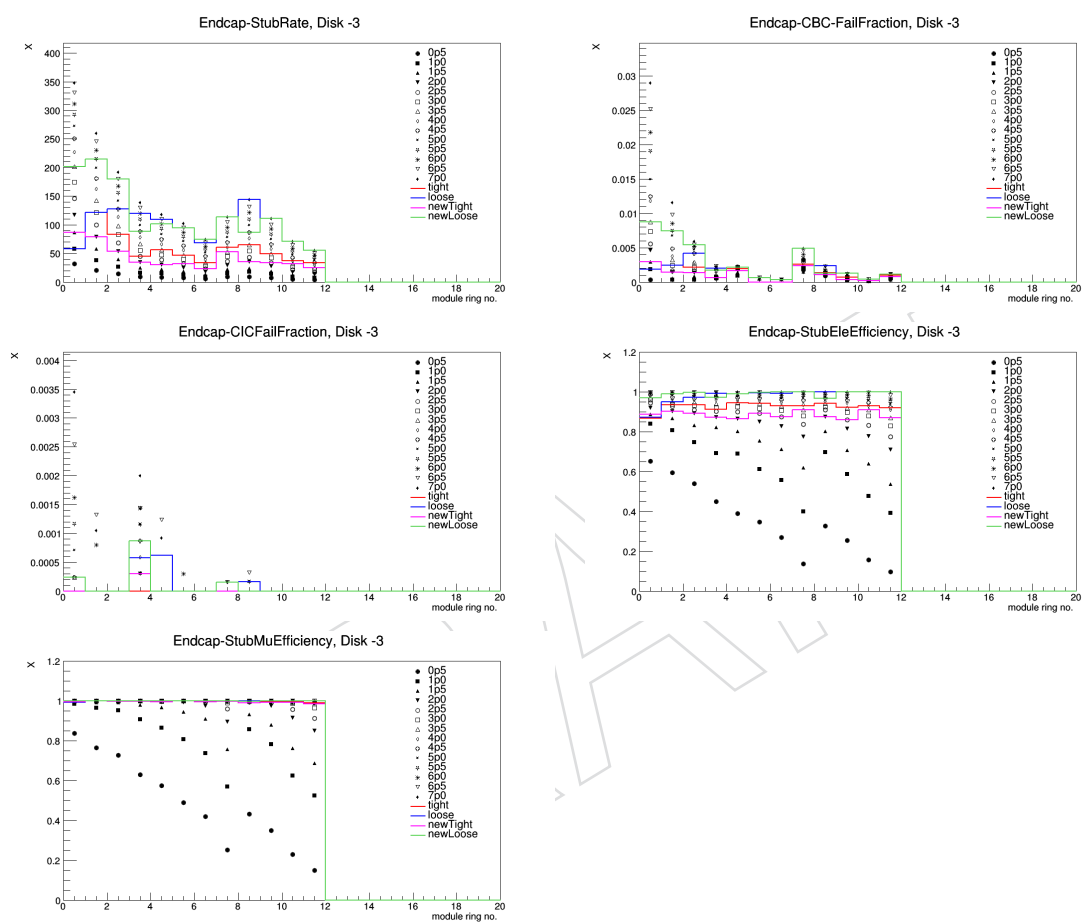


Figure 34: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in endcap disk 3.

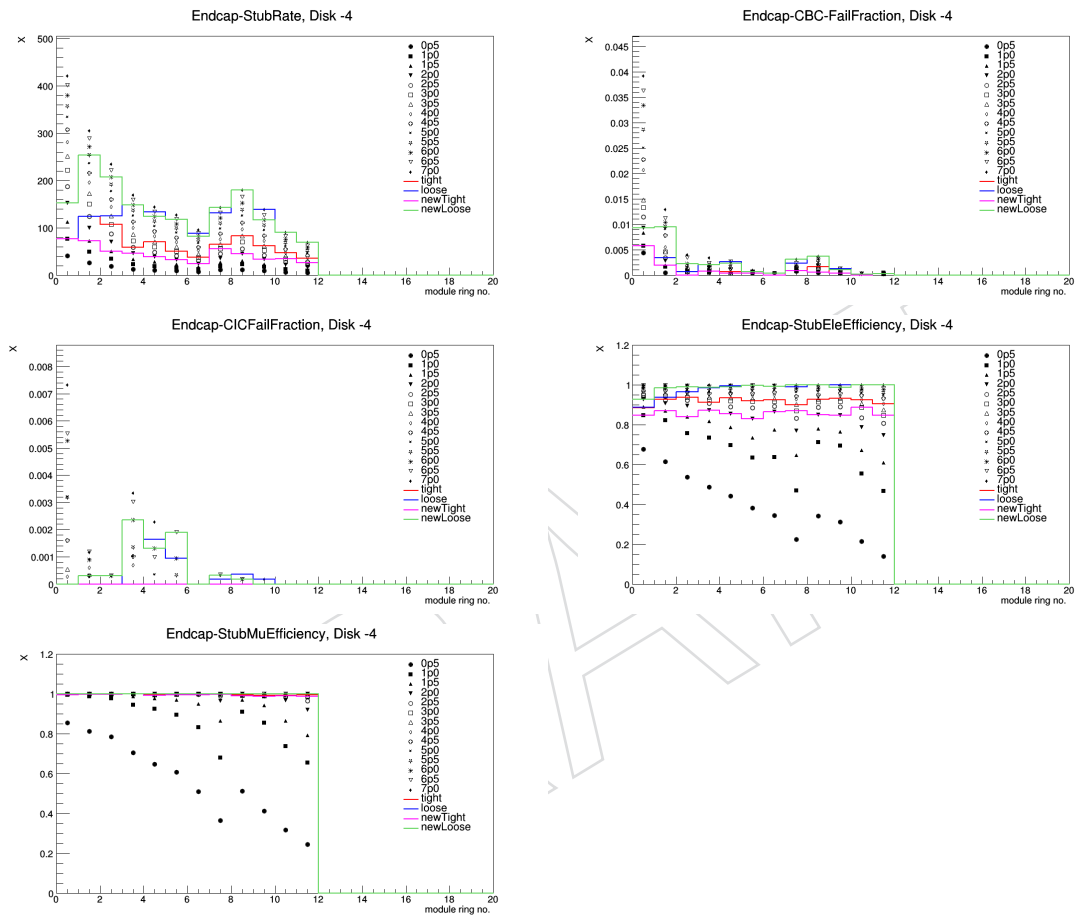


Figure 35: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in endcap disk 4.

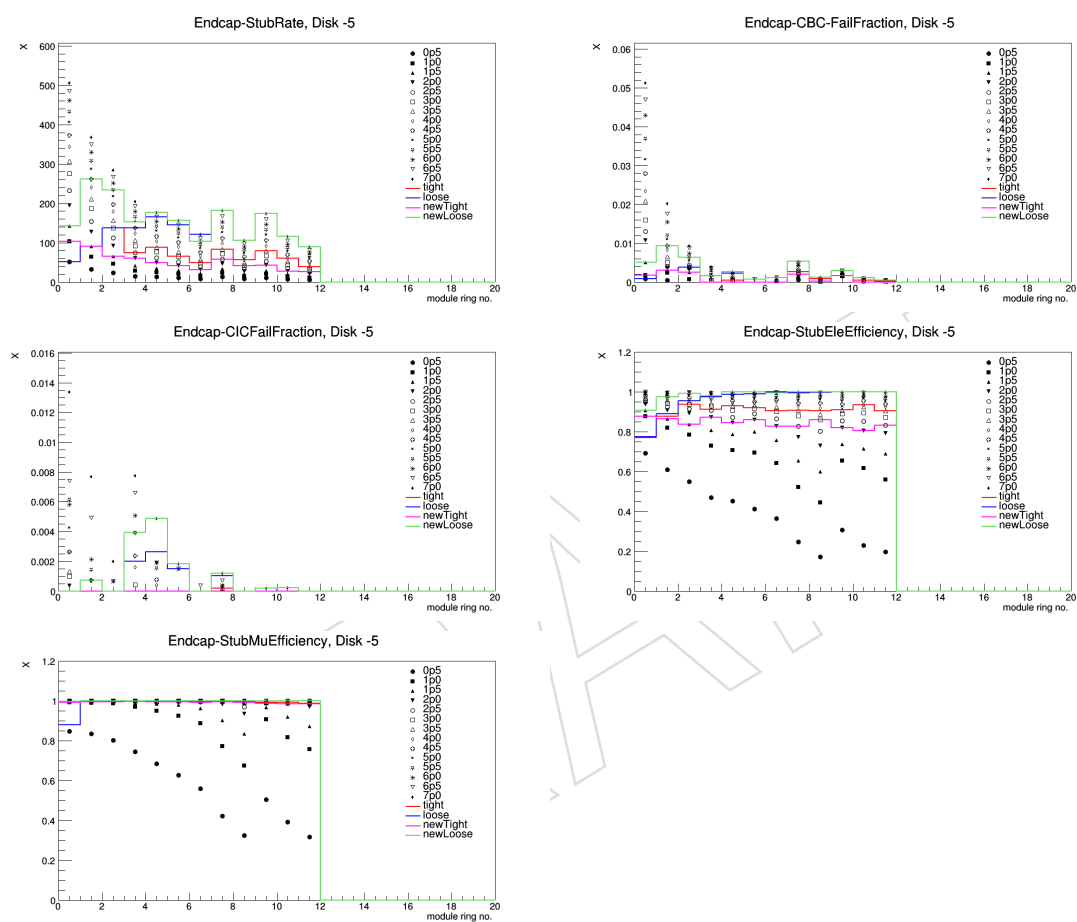


Figure 36: Distributions of stub rate (top left), CBC/MPA fail fraction (top right), CIC fail fraction (middle left), stub efficiency for electron (middle right), and stub efficiency for muon in endcap disk 5.

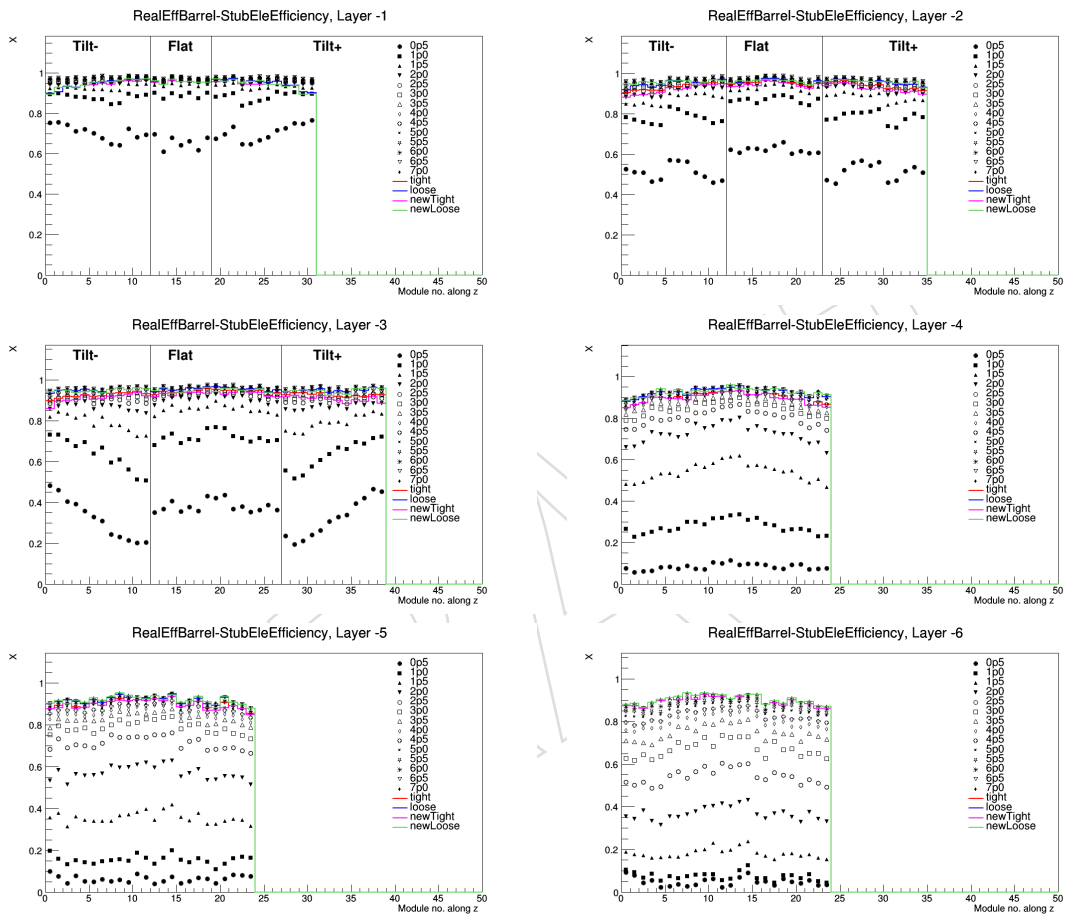


Figure 37: Distributions of stub efficiency for electron in Barrel layers.

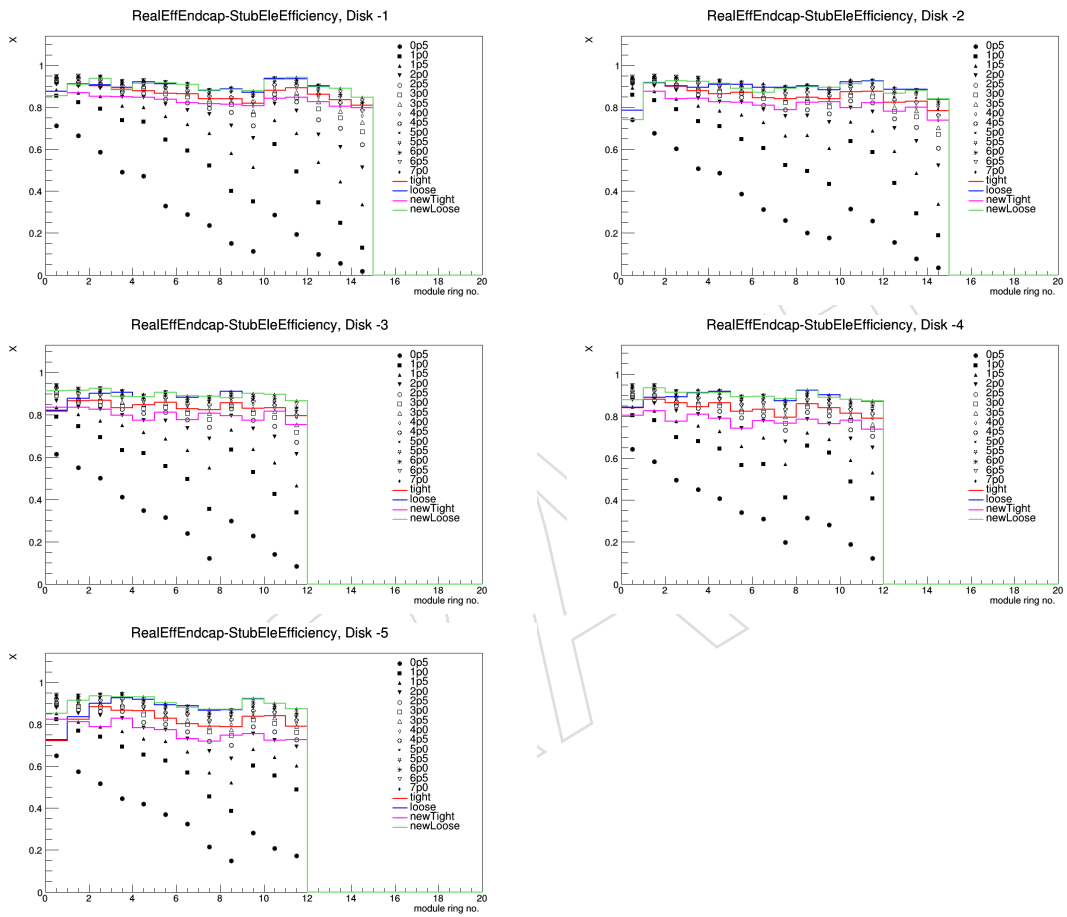


Figure 38: Distributions of stub efficiency for electron in endcaps layers.

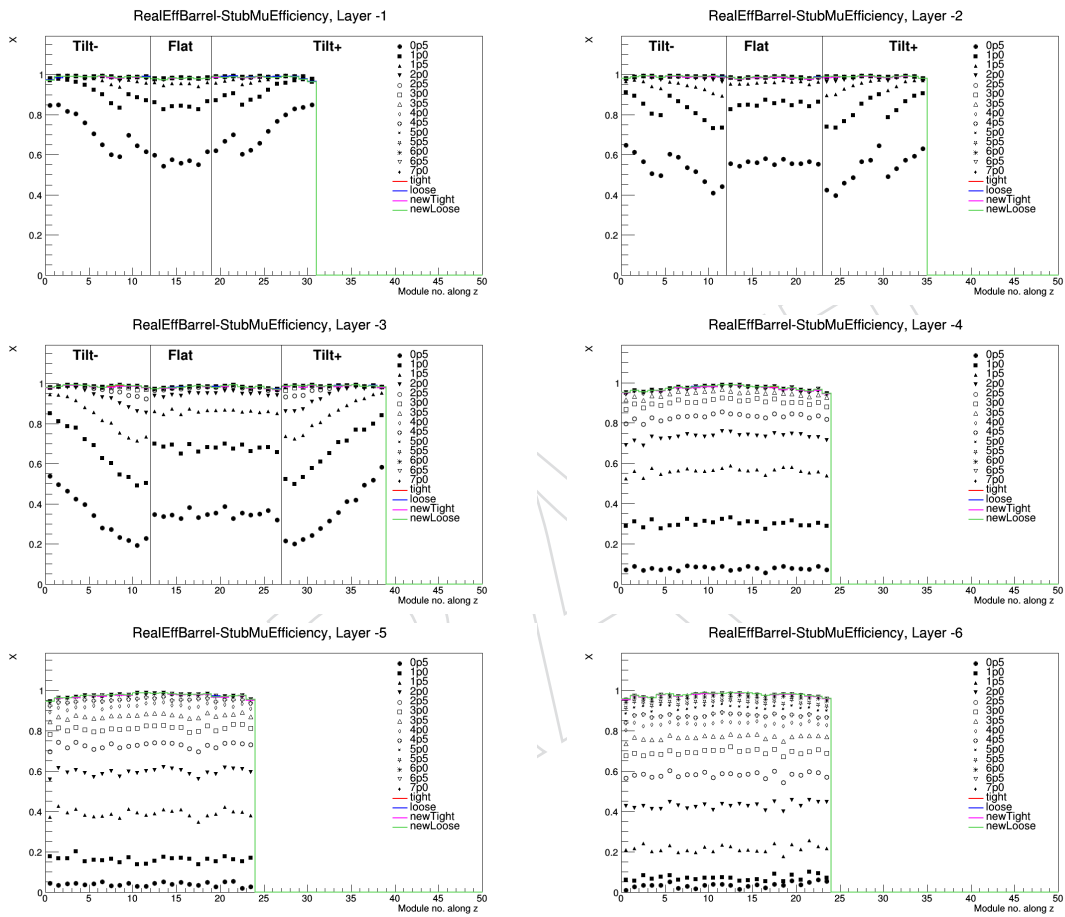


Figure 39: Distributions of stub efficiency for muon in Barrel layers.

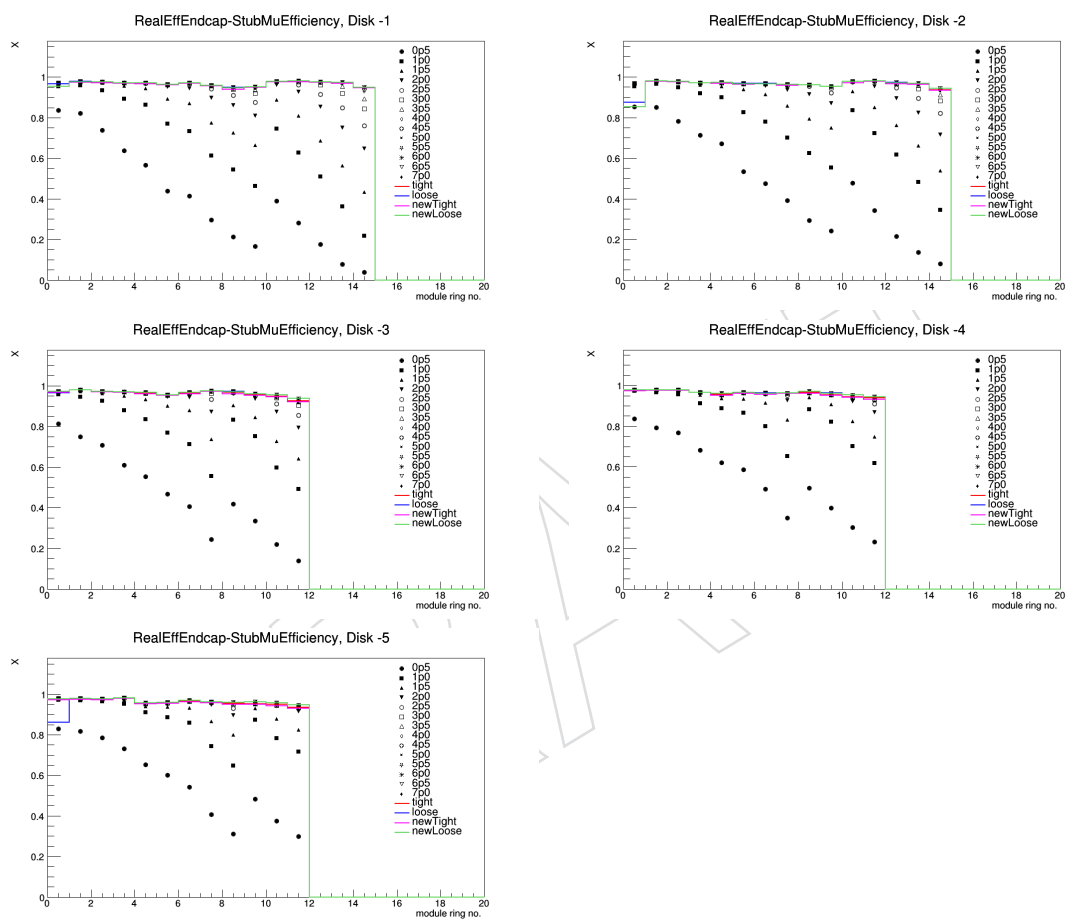


Figure 40: Distributions of stub efficiency for muon in endcaps layers.

7 Validation of the new stub window tunes

362

363 As shown in table 2, the new tight tune leads to the lowest stub rates while keeping the fail
 364 rates small enough. So it could be used instead of the current tune. Before using the new tune,
 365 we need to check the effect of the new tunes on the L1 track reconstruction efficiencies. In
 366 addition, since we have not included the displaced muon stub efficiency in the stub window
 367 optimisation procedure, we need to make sure that the L1 track efficiency is not degraded for
 368 displaced tracks.

369 In order to measure the track reconstruction efficiencies for different stub window tunes we
 370 have used the nominal L1 tracking Ntuple maker ¹ with the following changes:

```
371 in the L1Trigger/TrackFindingTracklet/test/L1TrackNtupleMaker_cfg.py file
372 TP_minNStub = cms.int32(0), # require TP to have >= X number of stubs associated with it
373 TP_minNStubLayer = cms.int32(0), # require TP to have stubs in >= X layers/disks
374 MCTruthClusterInputTag = cms.InputTag("TTClusterAssociatorFromPixelDigis", "ClusterInclusive")
```

375 In figures 41-43, track reconstruction efficiencies are shown for electron, muon, and tbar gen-
 376 eral tracks. All four available tunes are shown for two cases, with or without the ‘calcbendcut’
 377 (see section 5). In general, the old and new tunes show similar tracking efficiencies. Although
 378 the tight tune shows a bit higher efficiency (0.2%) compared to the new tight tune. It is worth
 379 mentioning that the ‘calcbendfix’ works since without the calcbend fix, the loose tunes have
 380 higher tracking efficiencies compared to the tight tunes.

381 In order to measure the L1 track reconstruction efficiency for displaced muon samples, we need
 382 to apply the following modifications in the L1 code;

```
383 in the L1Trigger/TrackFindingTracklet/test/L1TrackNtupleMaker_cfg.py file
384 L1TRKALGO = 'HYBRID_DISPLACED'
385 in the L1Trigger/TrackFindingTracklet/test/L1TrackNtuplePlot.C file
386 TP_minPt = 3.0, TP_maxEta = 2, TP_maxDxy = 10.0, TP_maxD0 = 10.0
```

387 In figure 45, track reconstruction efficiencies are shown for displaced muon tracks. All four
 388 available tunes are shown for two cases, with or without the ‘calcbendcut’ (see section 5). The
 389 new tight tune shows lower efficiency ($\approx 8\%$) compared to the tight tune. In figure 45, track
 390 reconstruction efficiencies are shown as a function of the track impact parameters (d_0 and z_0).
 391 The observed inefficiencies are related to the tracks with large d_0 (> 3 cm). In order to find
 392 the origin of the observed inefficiencies, we looked at the stub reconstruction efficiencies for
 393 displaced muons (see section 4). The stub reconstruction efficiencies for all displaced muon
 394 and displaced muon with $d_0 < 3$ cm are shown in figures 46 and 46 for barrel layers and
 395 endcap disks. The most affected regions are barrel layers 2 and 3 the most inner rings in the
 396 endcap disks. The L1 tracking efficiency for displaced muon as a function of η (see figure 44)
 397 shows that the L1 tracking efficiency at high η are not highly affected. Therefore the L1 track
 398 efficiencies for displaced muons are affected by tighter window sizes in barrel layers 2 and 3 in
 399 the new tight tune compared to the tight tune. We found that by widening the stub window
 400 sizes in barrel layers 2 and 3 of the new tight tune, we can restore the efficiency. Therefore, we
 401 made a new tune called “Modified tight tune” as the following

```
402 # New modified tight tune based on simulated events CMSSW_11_3_0_pre3, D76
403 BarrelCut = cms.vdouble(0, 2.0, 2.5, 3.5, 4.0, 5.5, 6.5),
404 TiltedBarrelCutSet = cms.VPSet(
405   cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
406   cms.PSet( TiltedCut = cms.vdouble( 0, 2.0, 2.0, 2.0, 2.0, 2.0, 2.0, 2.0, 1.5, 1.5, 1.5, 1.0, 1.0 ) ),
407   cms.PSet( TiltedCut = cms.vdouble( 0, 3.0, 3.0, 3.0, 3.0, 3.0, 3.0, 2.5, 2.5, 3.0, 3.0, 2.5, 2.5 ) ),
408   cms.PSet( TiltedCut = cms.vdouble(0, 4.0, 4.0, 4.0, 3.5, 3.5, 3.5, 3.0, 3.0, 2.5, 2.5, 2.5, 2.5) ),
409 ),
410 EndcapCutSet = cms.VPSet(
```

¹<https://twiki.cern.ch/twiki/bin/view/CMS/L1TrackSoftware>

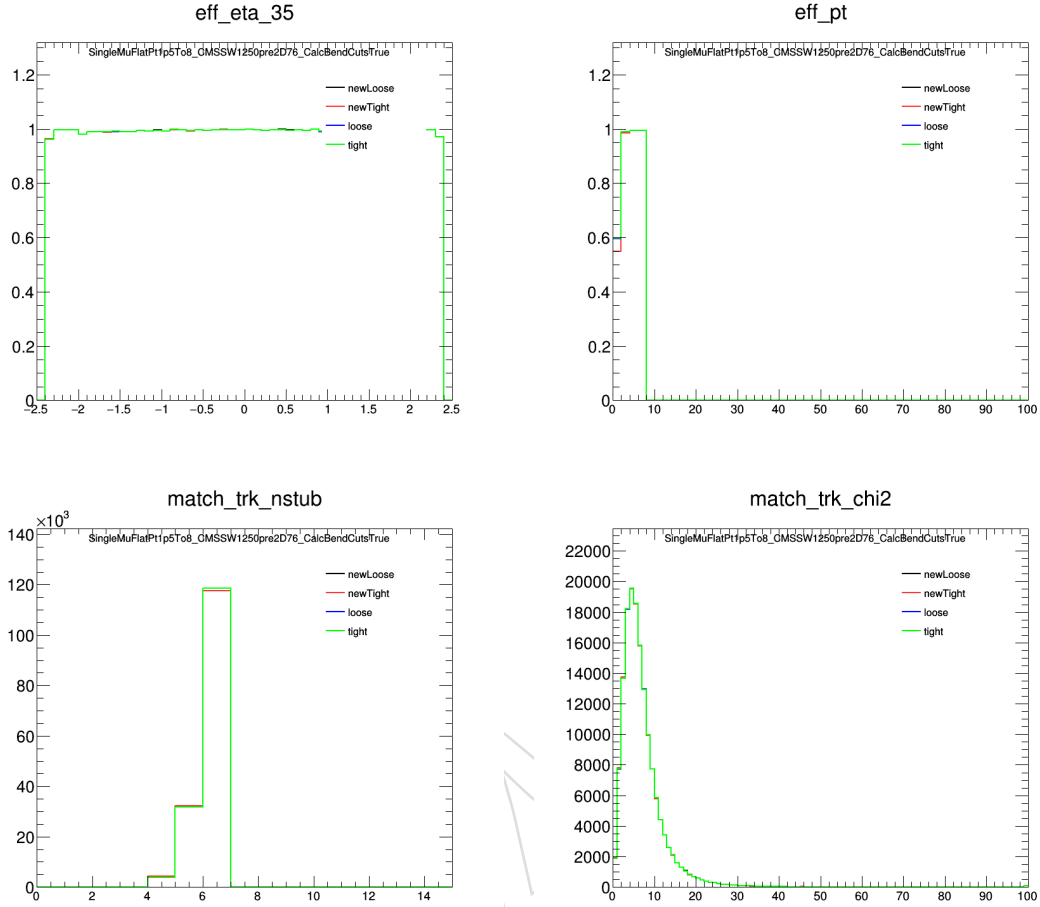
```
411     cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
412     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.5, 2.5, 3.0, 4.0, 4.0, 2.5, 3.0, 3.5, 4.0, 5.0) ),
413     cms.PSet( EndcapCut = cms.vdouble(0, 0.5, 1.5, 1.5, 2.0, 2.0, 2.0, 2.5, 2.5, 3.0, 3.5, 2.0, 2.5, 3.0, 4.0, 4.0) ),
414     cms.PSet( EndcapCut = cms.vdouble(0, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 3.0, 3.5, 2.5, 2.5, 3.0, 3.5) ),
415     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 3.0, 2.0, 2.0, 3.0, 3.0) ),
416     cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 3.0, 2.0, 2.0, 2.5) ),
417 )
418 \
```

419 In figure 48, L1 track reconstruction efficiencies are shown as a function of the track parameter
420 including the new modified tight tune. The efficiency loss at high d_0 are restored. So the new
421 modified tight tune passes all validation tests.

DRAFT

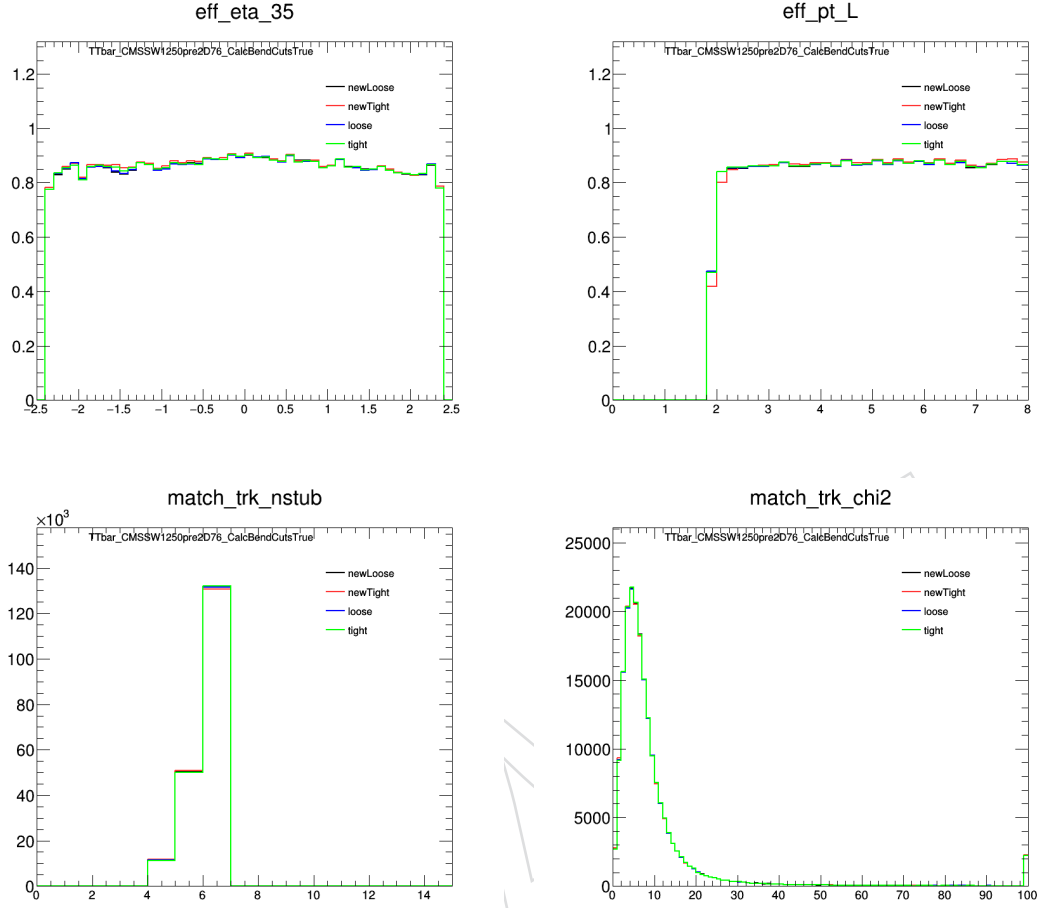


Figure 41: L1 track reconstruction efficiency for electrons with four available tunes and the 'calcBendCut' variable true or false .



Calc Bend Cuts	efficiency			
	newLoose	newTight	loose	tight
True	efficiency for $ \eta < 1.0 = 99.5461 \pm 0.0263692$ efficiency for $1.0 < \eta < 1.75 = 99.2919 \pm 0.0379305$ efficiency for $1.75 < \eta < 2.4 = 98.9149 \pm 0.0509313$ combined efficiency for $ \eta < 2.4 = 99.2978 \pm 0.0211936 = 154141/155231$	efficiency for $ \eta < 1.0 = 99.3429 \pm 0.0316924$ efficiency for $1.0 < \eta < 1.75 = 99.0893 \pm 0.0430577$ efficiency for $1.75 < \eta < 2.4 = 98.8835 \pm 0.0516552$ combined efficiency for $ \eta < 2.4 = 99.1393 \pm 0.0234449 = 153995/155231$	efficiency for $ \eta < 1.0 = 99.563 \pm 0.025875$ efficiency for $1.0 < \eta < 1.75 = 99.3042 \pm 0.0376026$ efficiency for $1.75 < \eta < 2.4 = 98.9149 \pm 0.0509313$ combined efficiency for $ \eta < 2.4 = 99.3088 \pm 0.0210289 = 154156/155231$	efficiency for $ \eta < 1.0 = 99.5588 \pm 0.0260599$ efficiency for $1.0 < \eta < 1.75 = 99.2878 \pm 0.0380391$ efficiency for $1.75 < \eta < 2.4 = 98.9342 \pm 0.0504805$ combined efficiency for $ \eta < 2.4 = 99.3062 \pm 0.0210677 = 154154/155231$
	efficiency for $pt > 2 = 99.2978 \pm 0.0211936$ efficiency for $2 < pt < 8.0 = 99.2978 \pm 0.0211936$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56939 # tracks/event (pt > 3.0) = 1.31165 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.1393 \pm 0.0234449$ efficiency for $2 < pt < 8.0 = 99.1393 \pm 0.0234449$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56722 # tracks/event (pt > 3.0) = 1.31123 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.3088 \pm 0.0210289$ efficiency for $2 < pt < 8.0 = 99.3088 \pm 0.0210289$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56939 # tracks/event (pt > 3.0) = 1.31113 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.3062 \pm 0.0210677$ efficiency for $2 < pt < 8.0 = 99.3062 \pm 0.0210677$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56963 # tracks/event (pt > 3.0) = 1.31159 # tracks/event (pt > 10.0) = 0
False	efficiency for $ \eta < 1.0 = 99.0983 \pm 0.0370813$ efficiency for $1.0 < \eta < 1.75 = 98.1139 \pm 0.042394$ efficiency for $1.75 < \eta < 2.4 = 98.8786 \pm 0.0517855$ combined efficiency for $ \eta < 2.4 = 99.0447 \pm 0.0246892 = 153748/155231$	efficiency for $ \eta < 1.0 = 99.3229 \pm 0.0321881$ efficiency for $1.0 < \eta < 1.75 = 99.0382 \pm 0.0441514$ efficiency for $1.75 < \eta < 2.4 = 98.7167 \pm 0.0583315$ combined efficiency for $ \eta < 2.4 = 99.0717 \pm 0.0243404 = 153790/155231$	efficiency for $ \eta < 1.0 = 99.126 \pm 0.0365124$ efficiency for $1.0 < \eta < 1.75 = 99.0771 \pm 0.0432581$ efficiency for $1.75 < \eta < 2.4 = 98.7771 \pm 0.0540299$ combined efficiency for $ \eta < 2.4 = 99.0176 \pm 0.025033 = 153706/155231$	efficiency for $ \eta < 1.0 = 99.5722 \pm 0.0256014$ efficiency for $1.0 < \eta < 1.75 = 99.2674 \pm 0.0385779$ efficiency for $1.75 < \eta < 2.4 = 98.7354 \pm 0.0545023$ combined efficiency for $ \eta < 2.4 = 99.2885 \pm 0.0217742 = 154080/155231$
	efficiency for $pt > 2 = 99.0447 \pm 0.0246892$ efficiency for $2 < pt < 8.0 = 99.0447 \pm 0.0246892$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56585 # tracks/event (pt > 3.0) = 1.31119 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.0717 \pm 0.0243404$ efficiency for $2 < pt < 8.0 = 99.0717 \pm 0.0243404$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56822 # tracks/event (pt > 3.0) = 1.31025 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.0176 \pm 0.025033$ efficiency for $2 < pt < 8.0 = 99.0176 \pm 0.025033$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56822 # tracks/event (pt > 3.0) = 1.31104 # tracks/event (pt > 10.0) = 0	efficiency for $pt > 2 = 99.2885 \pm 0.0217742$ efficiency for $2 < pt < 8.0 = 99.2885 \pm 0.0217742$ # TP/event (pt > 2) = 1.55231 # TP/event (pt > 3.0) = 1.29356 # TP/event (pt > 10.0) = 0 # tracks/event (pt > 2) = 1.56916 # tracks/event (pt > 3.0) = 1.31092 # tracks/event (pt > 10.0) = 0

Figure 42: L1 track reconstruction efficiency for muons with four available tunes and the 'calcBendCut' variable true or false.



Calc Bend Cuts	efficiency			
	newLoose	newTight	loose	tight
True	efficiency for $ \eta < 1.0 = 87.6161 \pm 0.0949411$ efficiency for $1.0 < \eta < 1.75 = 86.2469 \pm 0.137676$ efficiency for $1.75 < \eta < 2.4 = 83.4776 \pm 0.193126$ combined efficiency for $ \eta < 2.4 = 86.2288 \pm 0.0728418 = 19291/223801$ efficiency for $pt > 2 = 86.2288 \pm 0.0728418$ efficiency for $2 < pt < 8.0 = 86.1797 \pm 0.0840724$ efficiency for $pt > 8.0 = 86.3785 \pm 0.148872$ efficiency for $pt > 40.0 = 87.9521 \pm 0.036676$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 167.025 # tracks/event (pt > 3.0) = 58.7363 # tracks/event (pt > 10.0) = 5.03533	efficiency for $ \eta < 1.0 = 87.6086 \pm 0.0949557$ efficiency for $1.0 < \eta < 1.75 = 85.5178 \pm 0.136924$ efficiency for $1.75 < \eta < 2.4 = 83.8588 \pm 0.191319$ combined efficiency for $ \eta < 2.4 = 86.3682 \pm 0.0725307 = 193293/223801$ efficiency for $pt > 2 = 86.3682 \pm 0.0725307$ efficiency for $2 < pt < 8.0 = 86.0693 \pm 0.0843534$ efficiency for $pt > 8.0 = 87.2791 \pm 0.1417$ efficiency for $pt > 40.0 = 86.9535 \pm 0.490971$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 164.54 # tracks/event (pt > 3.0) = 58.3723 # tracks/event (pt > 10.0) = 5.02678	efficiency for $ \eta < 1.0 = 87.5621 \pm 0.0951186$ efficiency for $1.0 < \eta < 1.75 = 85.2574 \pm 0.137536$ efficiency for $1.75 < \eta < 2.4 = 83.8316 \pm 0.192871$ combined efficiency for $ \eta < 2.4 = 86.2119 \pm 0.0728795 = 192943/223801$ efficiency for $pt > 2 = 86.2119 \pm 0.0728795$ efficiency for $2 < pt < 8.0 = 86.1708 \pm 0.0840951$ efficiency for $pt > 8.0 = 86.3369 \pm 0.146059$ efficiency for $pt > 40.0 = 87.8768 \pm 0.510208$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 167.218 # tracks/event (pt > 3.0) = 58.7973 # tracks/event (pt > 10.0) = 5.02222	efficiency for $ \eta < 1.0 = 87.7208 \pm 0.0945955$ efficiency for $1.0 < \eta < 1.75 = 85.6066 \pm 0.136175$ efficiency for $1.75 < \eta < 2.4 = 83.6119 \pm 0.19254$ combined efficiency for $ \eta < 2.4 = 86.4125 \pm 0.0724315 = 193293/223801$ efficiency for $pt > 2 = 86.4125 \pm 0.0724315$ efficiency for $2 < pt < 8.0 = 86.3334 \pm 0.0836781$ efficiency for $pt > 8.0 = 86.6334 \pm 0.144622$ efficiency for $pt > 40.0 = 86.901 \pm 0.507983$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 167.046 # tracks/event (pt > 3.0) = 58.5893 # tracks/event (pt > 10.0) = 5.0711
False	efficiency for $ \eta < 1.0 = 88.7029 \pm 0.100892$ efficiency for $1.0 < \eta < 1.75 = 84.5977 \pm 0.140071$ efficiency for $1.75 < \eta < 2.4 = 83.4181 \pm 0.193403$ combined efficiency for $ \eta < 2.4 = 84.9943 \pm 0.0754905 = 190218/223801$ efficiency for $pt > 2 = 84.9943 \pm 0.0754905$ efficiency for $2 < pt < 8.0 = 84.7264 \pm 0.0876341$ efficiency for $pt > 8.0 = 85.3106 \pm 0.148391$ efficiency for $pt > 40.0 = 86.9746 \pm 0.526186$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 164.019 # tracks/event (pt > 3.0) = 58.7816 # tracks/event (pt > 10.0) = 5.04657	efficiency for $ \eta < 1.0 = 87.6136 \pm 0.0949493$ efficiency for $1.0 < \eta < 1.75 = 85.3477 \pm 0.137189$ efficiency for $1.75 < \eta < 2.4 = 83.8592 \pm 0.19222$ combined efficiency for $ \eta < 2.4 = 86.2892 \pm 0.0727075 = 193116/223801$ efficiency for $pt > 2 = 86.2892 \pm 0.0727075$ efficiency for $2 < pt < 8.0 = 86.0848 \pm 0.0843142$ efficiency for $pt > 8.0 = 86.912 \pm 0.143428$ efficiency for $pt > 40.0 = 86.2698 \pm 0.503027$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 164.425 # tracks/event (pt > 3.0) = 58.3044 # tracks/event (pt > 10.0) = 5.39127	efficiency for $ \eta < 1.0 = 85.6165 \pm 0.101145$ efficiency for $1.0 < \eta < 1.75 = 84.3878 \pm 0.140811$ efficiency for $1.75 < \eta < 2.4 = 83.3523 \pm 0.193568$ combined efficiency for $ \eta < 2.4 = 84.8826 \pm 0.0757212 = 189968/223801$ efficiency for $pt > 2 = 84.8826 \pm 0.0757212$ efficiency for $2 < pt < 8.0 = 84.6189 \pm 0.0878859$ efficiency for $pt > 8.0 = 85.6859 \pm 0.148934$ efficiency for $pt > 40.0 = 86.9015 \pm 0.527454$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 163.895 # tracks/event (pt > 3.0) = 58.398 # tracks/event (pt > 10.0) = 5.07344	efficiency for $ \eta < 1.0 = 87.5579 \pm 0.0951322$ efficiency for $1.0 < \eta < 1.75 = 85.4486 \pm 0.136794$ efficiency for $1.75 < \eta < 2.4 = 83.41 \pm 0.193441$ combined efficiency for $ \eta < 2.4 = 86.2463 \pm 0.072803 = 193020/223801$ efficiency for $pt > 2 = 86.2463 \pm 0.072803$ efficiency for $2 < pt < 8.0 = 86.2444 \pm 0.0839089$ efficiency for $pt > 8.0 = 86.2819 \pm 0.146441$ efficiency for $pt > 40.0 = 87.4578 \pm 0.517217$ # TP/event (pt > 2) = 175.946 # TP/event (pt > 3.0) = 58.3381 # TP/event (pt > 10.0) = 5.076 # tracks/event (pt > 2) = 166.983 # tracks/event (pt > 3.0) = 58.6621 # tracks/event (pt > 10.0) = 5.09222

Figure 43: L1 track reconstruction efficiency for ttbar tracks with four available tunes and the 'calcBendCut' variable true or false.



Figure 44: L1 track reconstruction efficiency for displaced muons with four available tunes and the 'calcBendCut' variable true or false.

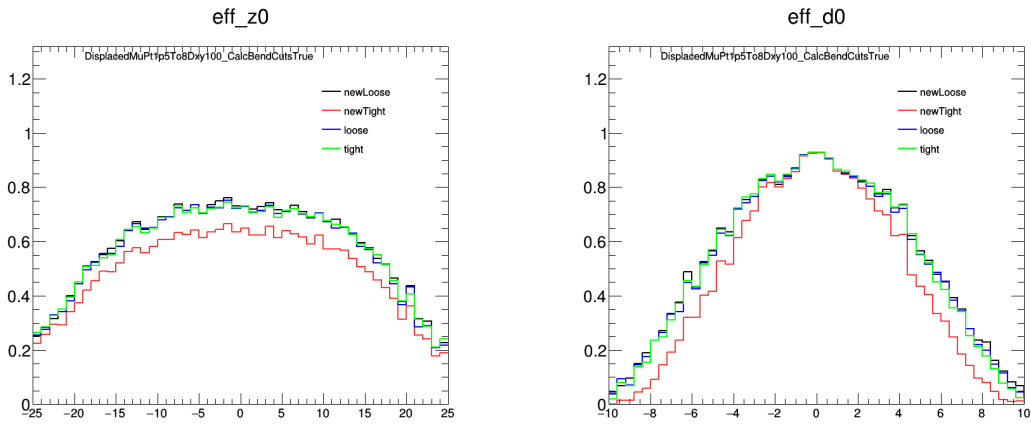


Figure 45: L1 track reconstruction efficiency for displaced muons as a function of the track impact parameters with four available tunes.

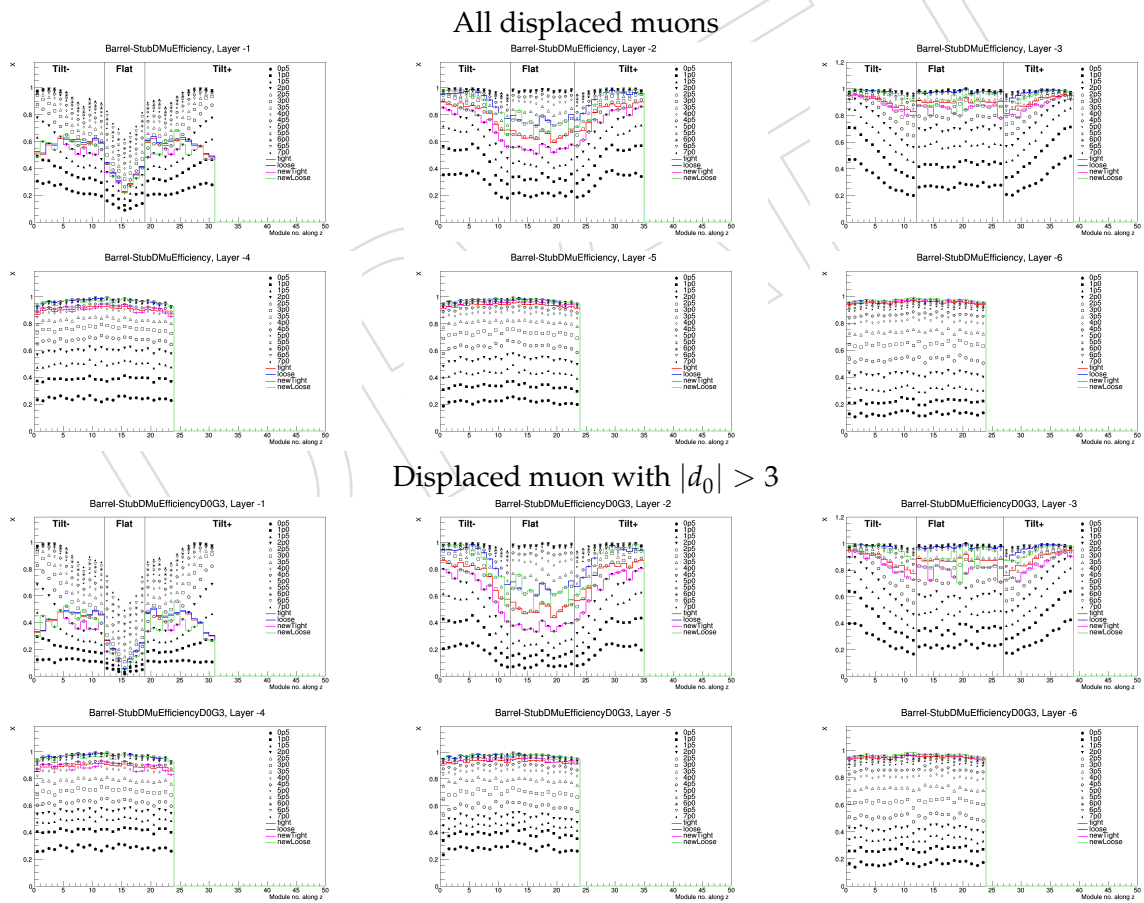


Figure 46: Stub reconstruction efficiencies in barrel layers for all displaced muon (top) and displaced muon with $|d_0| > 3$ cm (bottom) in barrel layers.

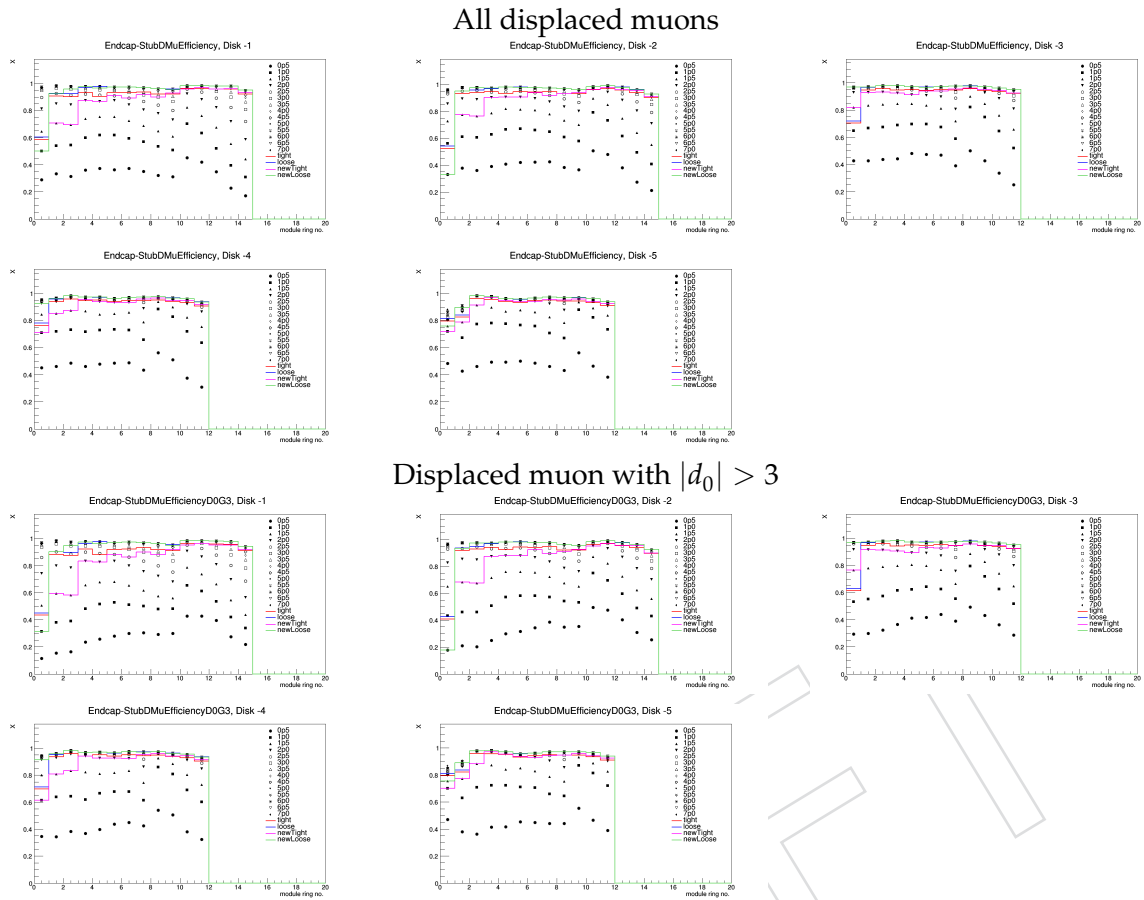


Figure 47: Stub reconstruction efficiencies in barrel layers for all displaced muon (top) and displaced muon with $|d_0| > 3$ cm (bottom) in endcap disks.

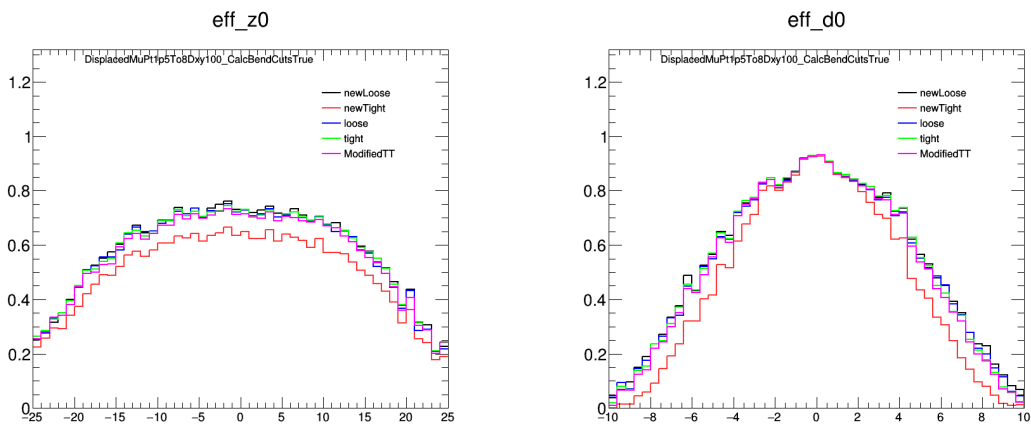


Figure 48: L1 track reconstruction efficiency for displaced muons as a function of the track impact parameters with four available tunes.

8 Summary

422

423 A new CMS Tracker is under development for operation at the High Luminosity LHC. It in-
424 cludes an outer tracker based on dedicated modules that will reconstruct short track segments,
425 called stubs, using spatially coincident clusters in two closely spaced silicon sensor layers. In
426 this detector note, we studied various properties of the stubs using the latest simulated sam-
427 ples. We have measured the stub rates, the fraction of stubs that are failed in data transmission
428 and stub reconstruction efficiencies. These stub properties depend directly on the stub window
429 size. We showed this dependency in various region of the tracker. We have developed an al-
430 gorithm to combine these properties and extract optimum widow sizes in all detector regions.
431 The final stub window tune that we propose to be used in the main L1 track trigger code is the
432 following;

```
433 # New modified tight tune based on simulated events CMSSW_11_3_0_pre3, D76
434 BarrelCut = cms.vdouble(0, 2.0, 2.5, 3.5, 4.0, 5.5, 6.5),
435 TiltedBarrelCutSet = cms.VPSet(
436   cms.PSet( TiltedCut = cms.vdouble( 0 ) ),
437   cms.PSet( TiltedCut = cms.vdouble( 0, 2.0, 2.0, 2.0, 2.0, 2.0, 2.0, 2.0, 1.5, 1.5, 1.5, 1.0, 1.0 ) ),
438   cms.PSet( TiltedCut = cms.vdouble( 0, 3.0, 3.0, 3.0, 3.0, 3.0, 3.0, 2.5, 2.5, 3.0, 3.0, 2.5, 2.5, 2.5 ) ),
439   cms.PSet( TiltedCut = cms.vdouble(0, 4.0, 4.0, 4.0, 3.5, 3.5, 3.5, 3.0, 3.0, 2.5, 2.5, 2.5, 2.5) ) ),
440 ),
441 EndcapCutSet = cms.VPSet(
442   cms.PSet( EndcapCut = cms.vdouble( 0 ) ),
443   cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.5, 2.5, 3.0, 4.0, 4.0, 2.5, 3.0, 3.5, 4.0, 5.0 ) ),
444   cms.PSet( EndcapCut = cms.vdouble(0, 0.5, 1.5, 1.5, 2.0, 2.0, 2.0, 2.5, 2.5, 3.0, 3.5, 2.0, 2.5, 3.0, 4.0, 4.0 ) ),
445   cms.PSet( EndcapCut = cms.vdouble(0, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 3.0, 3.5, 2.5, 2.5, 3.0, 3.5 ) ),
446   cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 3.0, 2.0, 2.0, 3.0, 3.0 ) ),
447   cms.PSet( EndcapCut = cms.vdouble(0, 1.0, 1.5, 1.5, 2.0, 2.0, 2.0, 2.0, 2.5, 3.0, 2.0, 2.0, 2.5 ) ),
448 )
449 \
```

References

- 450 [1] D. Contardo et al., “Technical Proposal for the Phase-II Upgrade of the CMS Detector”,
452 Technical Report CERN-LHCC-2015-010. LHCC-P-008. CMS-TDR-15-02, Geneva, Jun,
453 2015. Upgrade Project Leader Deputies: Lucia Silvestris (INFN-Bari), Jeremy Mans
454 (University of Minnesota) Additional contacts: Lucia.Silvestris@cern.ch,
455 Jeremy.Mans@cern.ch.
- 456 [2] CMS Collaboration Collaboration, “The Phase-2 Upgrade of the CMS L1 Trigger Interim
457 Technical Design Report”, Technical Report CERN-LHCC-2017-013. CMS-TDR-017,
458 CERN, Geneva, Sep, 2017. This is the CMS Interim TDR devoted to the upgrade of the
459 CMS L1 trigger in view of the HL-LHC running, as approved by the LHCC.
- 460 [3] CMS Collaboration Collaboration, “The Phase-2 Upgrade of the CMS Tracker”, Technical
461 Report CERN-LHCC-2017-009. CMS-TDR-014, CERN, Geneva, Jun, 2017.
- 462 [4] L. Caponetto, S. Viret, and Y. Zoccarato, “I/O data formats for the Concentrator Integrated
463 Circuit”,.
- 464 [5] S. Viret, “Stub definition and properties”, *CMS DN -2018/003* (2018).
- 465 [6] A. Ryd and L. Skinnari, “Tracking Triggers for the HL-LHC”, *Ann. Rev. Nucl. Part. Sci.* **70**
466 (2020) 171–195, doi:10.1146/annurev-nucl-020420-093547,
467 arXiv:2010.13557.

DRAFT