

Getting started with gcreg

Joshua Bon

2017-11-30

gcreg fits constrained regression models. The functionality and documentation of this package is still being developed. Constrained polynomial regression models can be fitted with the function `cpm()`. This vignette will demonstrate some examples.

Monotonic Regression

Monotonicity is a constraint provided directly in `cpm()`. We will use some datasets from the `fda` package.

The `onechild` in `fda` (Tuddenham and Snyder, 1954):

```
library(fda)

## Loading required package: splines
## Loading required package: Matrix
##
## Attaching package: 'fda'
## The following object is masked from 'package:graphics':
##
##   matplot
library(ggplot2)

g_oc <- ggplot(data = fda::onechild) + geom_point(aes(y = height, x = day), size = 0.5) + theme_bw()

print(g_oc)
```

We can fit a constrained polynomial model and an unconstrained model for comparison:

```
library(gcreg)

## Loading required package: polynom
## Loading required package: dplyr
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##   filter, lag
## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union
library(dplyr)

deg <- 11

c_model <- cpm(height ~ day, data = fda::onechild, degree = deg,
```

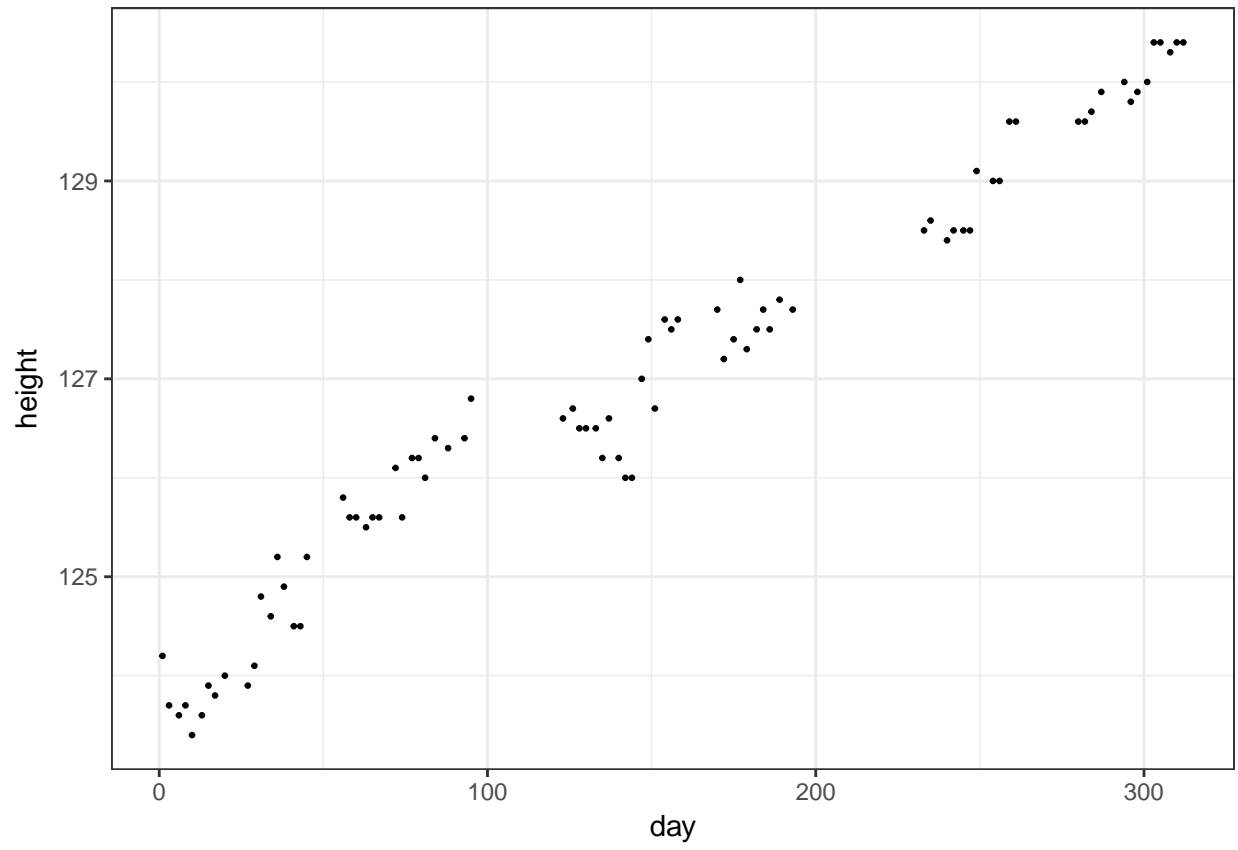


Figure 1: fda::onechild data

```

        constraint = "monotone", c_region = range(fda::onechild$day))

u_model <- lm(height ~ poly(day, degree = deg), data = fda::onechild)

# RSS
RSS <- list(
  c_model = sum(residuals(c_model)^2),
  u_model = sum(residuals(u_model)^2)
)

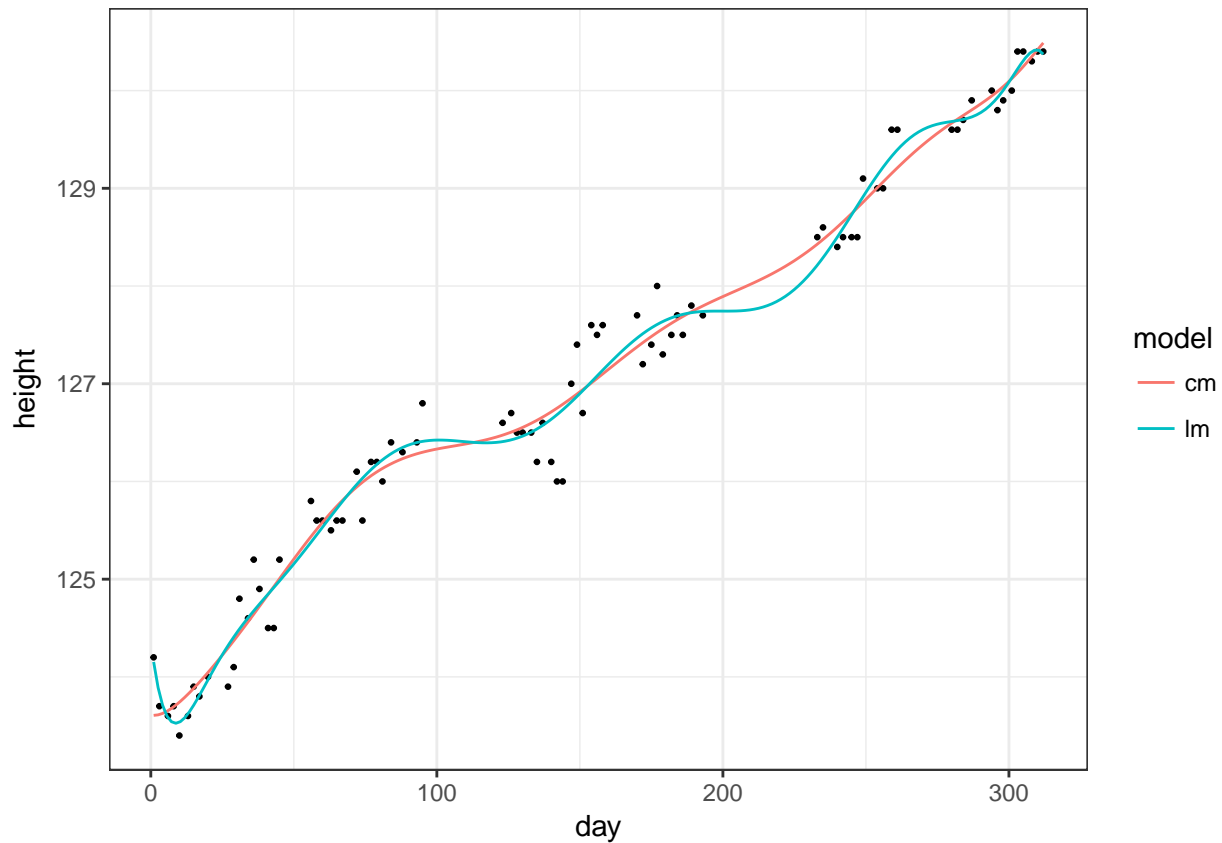
RSS

## $c_model
## [1] 6.556164
##
## $u_model
## [1] 5.595704

The fitted curves:
plot_dat <- with(fda::onechild, data.frame(day = seq(from = min(day), to = max(day), length.out = 201)))
c_plot_dat <- plot_dat %>% mutate(model = "cm", height = predict(c_model, newdata = plot_dat$day)[,1])
u_plot_dat <- plot_dat %>% mutate(model = "lm", height = predict(u_model, newdata = list(day=day)))
plot_dat <- rbind(c_plot_dat, u_plot_dat)

g_oc + geom_line(data = plot_dat, aes(y = height, x = day, colour = model))

```



User-defined constraints

Use the `make_oracle()` function to define your own constraints. This is still under development - speed may vary.

```
# Constraint: T if beta[3] >= 1, F otherwise
b3_g1 <- function(b){
  b[3,1] >= 1
}

deg <- 7

# Initial value
start_beta <- runif(n = deg + 1)
start_beta[3] <- 3

orc_f <- make_oracle(oracle = b3_g1)

c_model <- cpm(height ~ day, data = fda::onechild, degree = deg,
              oracle = orc_f, start = start_beta, step_start = 0.99, method = "down-walk")

c_model

##
## Constrained regression model
## Call:
```

```
## cpm(formula = height ~ day, data = fda::onechild, degree = deg,  
##      oracle = orc_f, start = start_beta, step_start = 0.99, method = "down-walk")  
##  
## Coefficients:  
## Intercept      x^1      x^2      x^3      x^4      x^5  
## 1.085e+03 -6.712e+01 1.000e+00 -5.109e-03 8.703e-06 -2.535e-09  
##      x^6      x^7  
## 5.454e-12 -4.668e-15
```